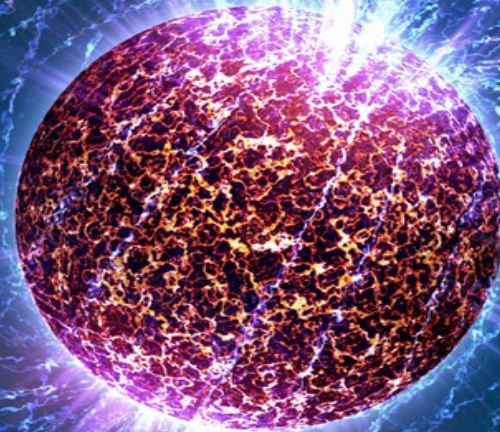


Particle acceleration and radiation in pulsars

New insights from PIC simulations



Benoît Cerutti

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Pulsars are rapidly-rotating, high-magnetized neutron stars

NATURE, VOL. 217, FEBRUARY 24, 1968

709

Observation of a Rapidly Pulsating Radio Source

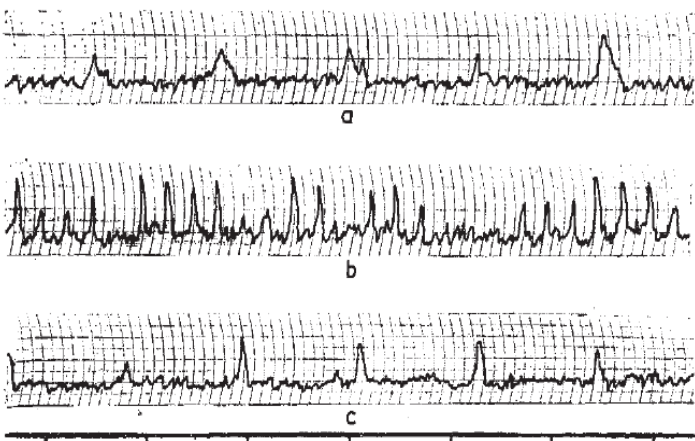
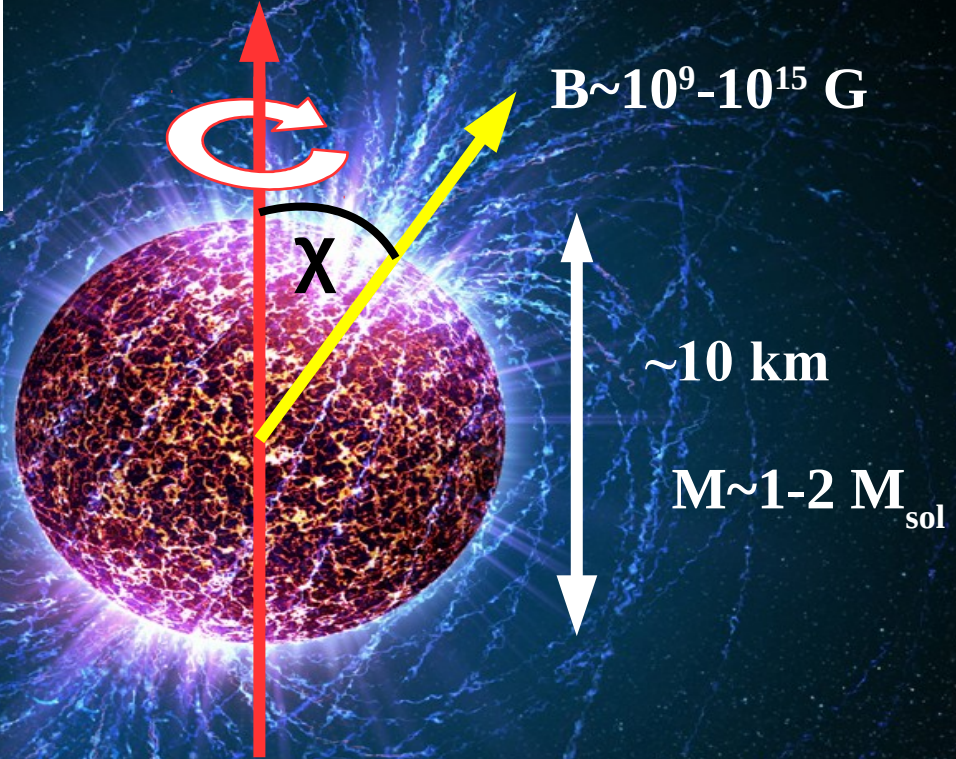
by

A. HEWISH
S. J. BELL
J. D. H. PILKINGTON
P. F. SCOTT
R. A. COLLINS

Unusual signals from pulsating radio sources have been recorded at the Mullard Radio Astronomy Observatory. The radiation seems to come from local objects within the galaxy, and may be associated with oscillations of white dwarf or neutron stars.

Mullard Radio Astronomy Observatory,
Cavendish Laboratory,
University of Cambridge

Spin period P : 1 ms – few seconds



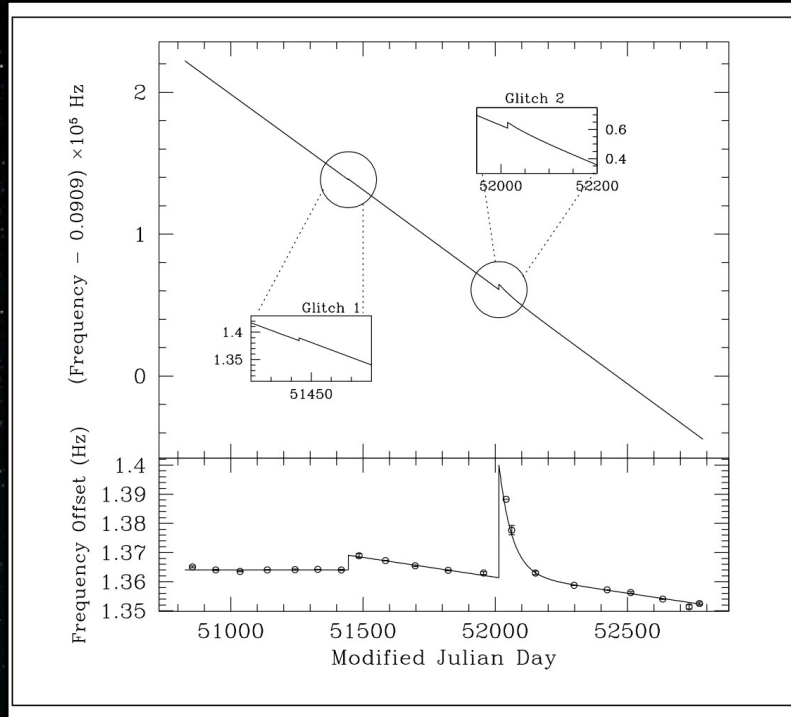
← Time increasing Seconds

Fig. 1. Pulses observed with a recording time constant of about 0.03 s on March 21, 1968. (a) CP.0834. (b) CP.0950, during a period of intense activity. (c) CP.1133.

Pulsars represent great laboratories to explore extreme physical conditions :

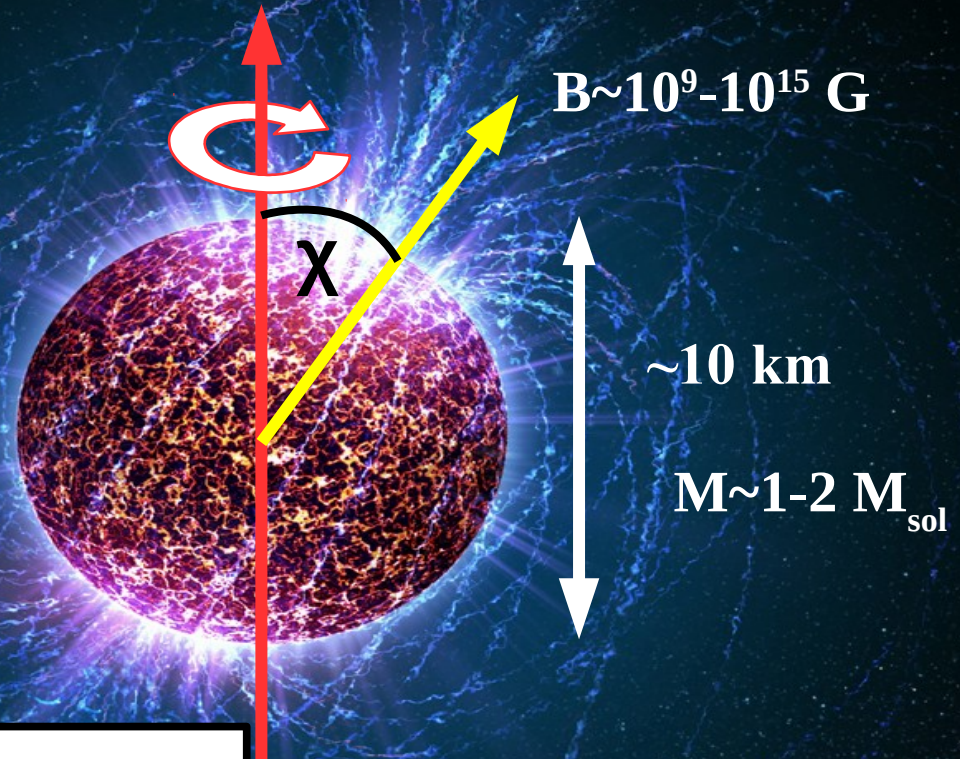
Extreme **electromagnetic** fields, test for **General Relativity**, **ultra-dense** matter (equation of state), **pair creation**, **particle acceleration** and **radiation**, **relativistic** outflows.

Pulsars slowdown



Kaspi & Gavril (2003)

Spin period P : 1 ms – few seconds



Measured with high-accuracy :

P : rotation period

Gives the total **rotational energy** available

dP/dt : period slowdown (increase)

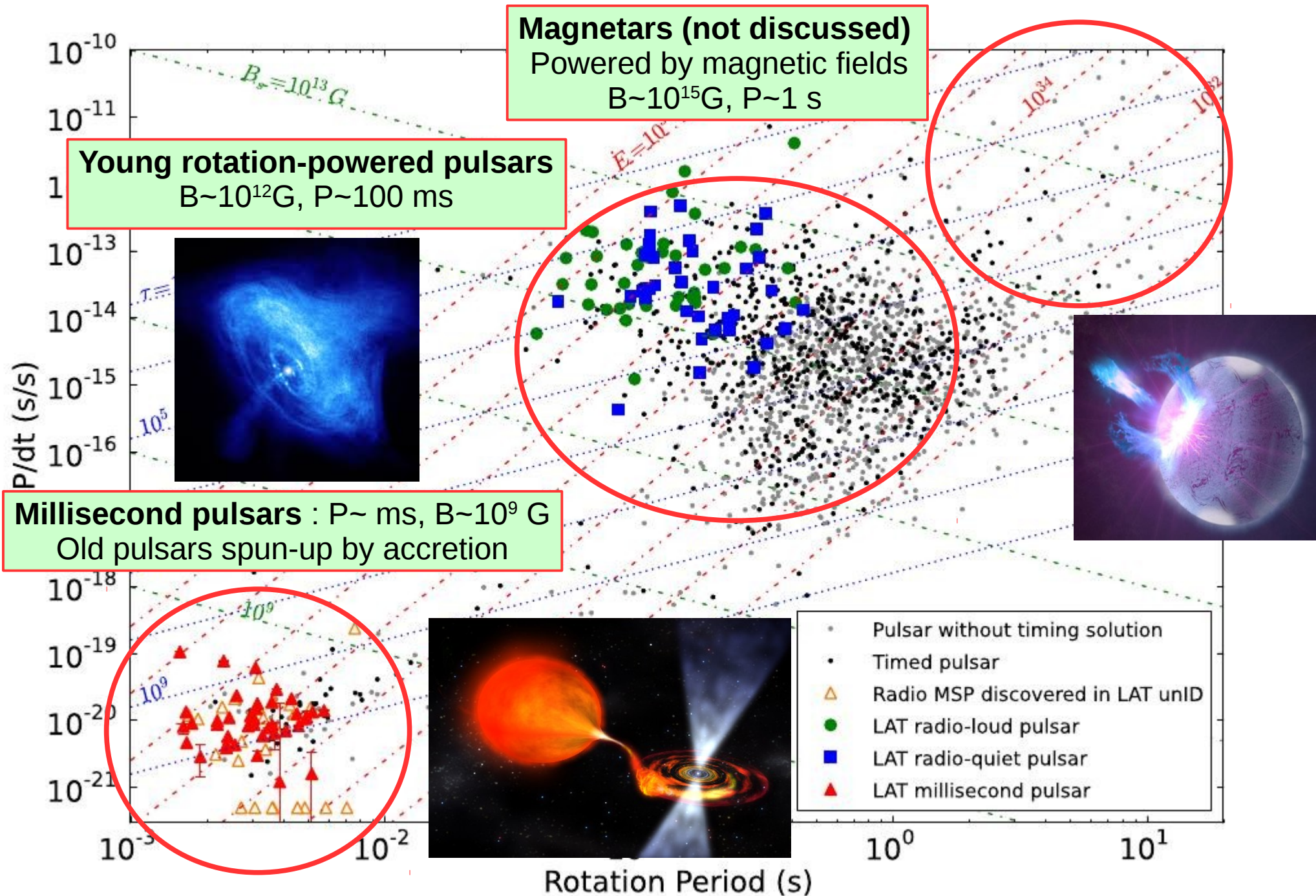
Gives the total **power release** (seen and unseen !)

For a magnetic dipole in vacuum :

- Age : $T \propto P / \dot{P}$

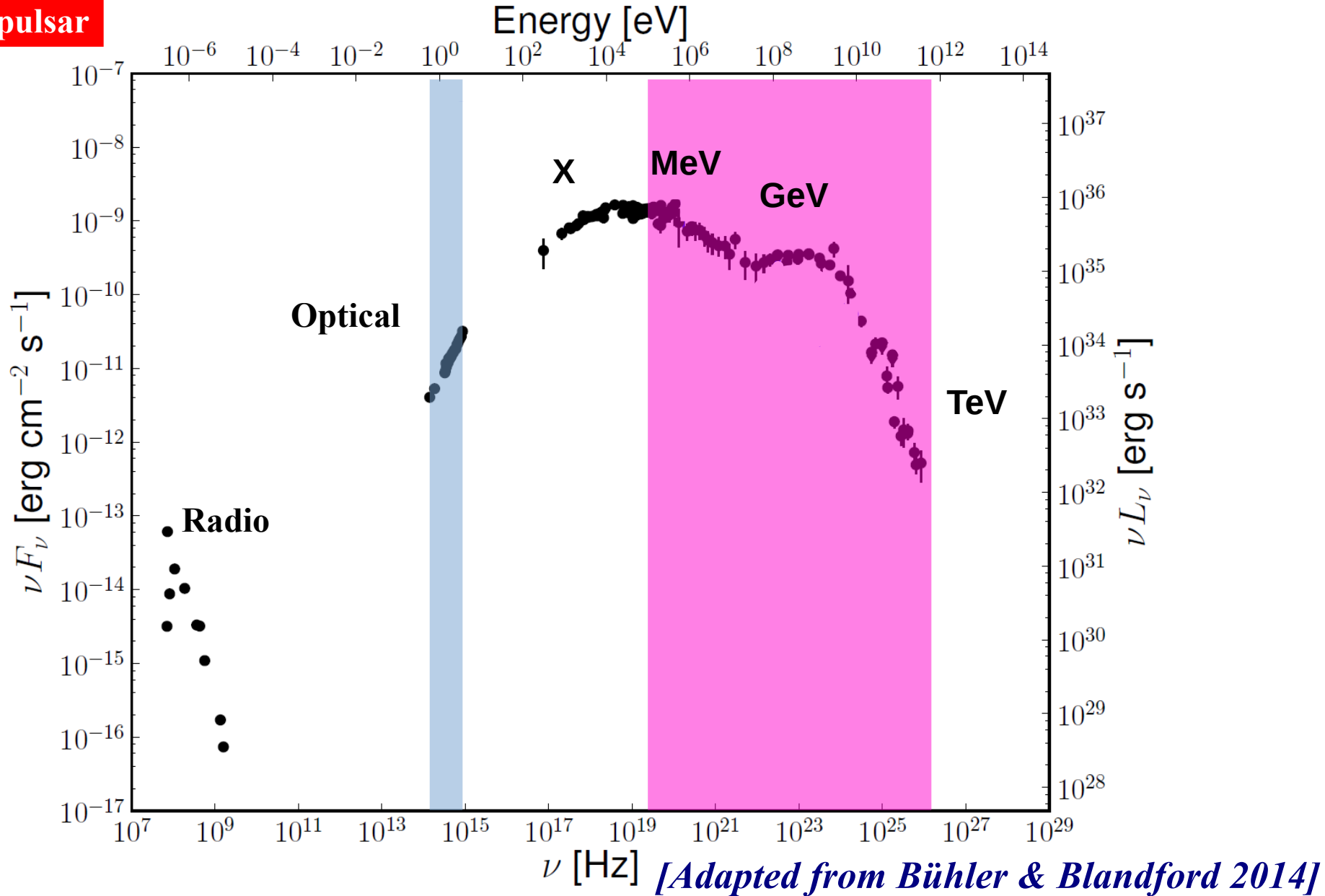
- Magnetic field : $B \sin \chi \propto \sqrt{P \dot{P}}$

The P-Pdot diagram : The HR diagram for pulsars



Pulsars shine throughout the electromagnetic spectrum

The Crab pulsar

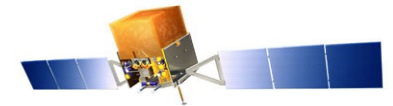


A large fraction of the pulsar spindown is released in light, in particular in the **gamma-ray band**. => **Efficient particle acceleration !**

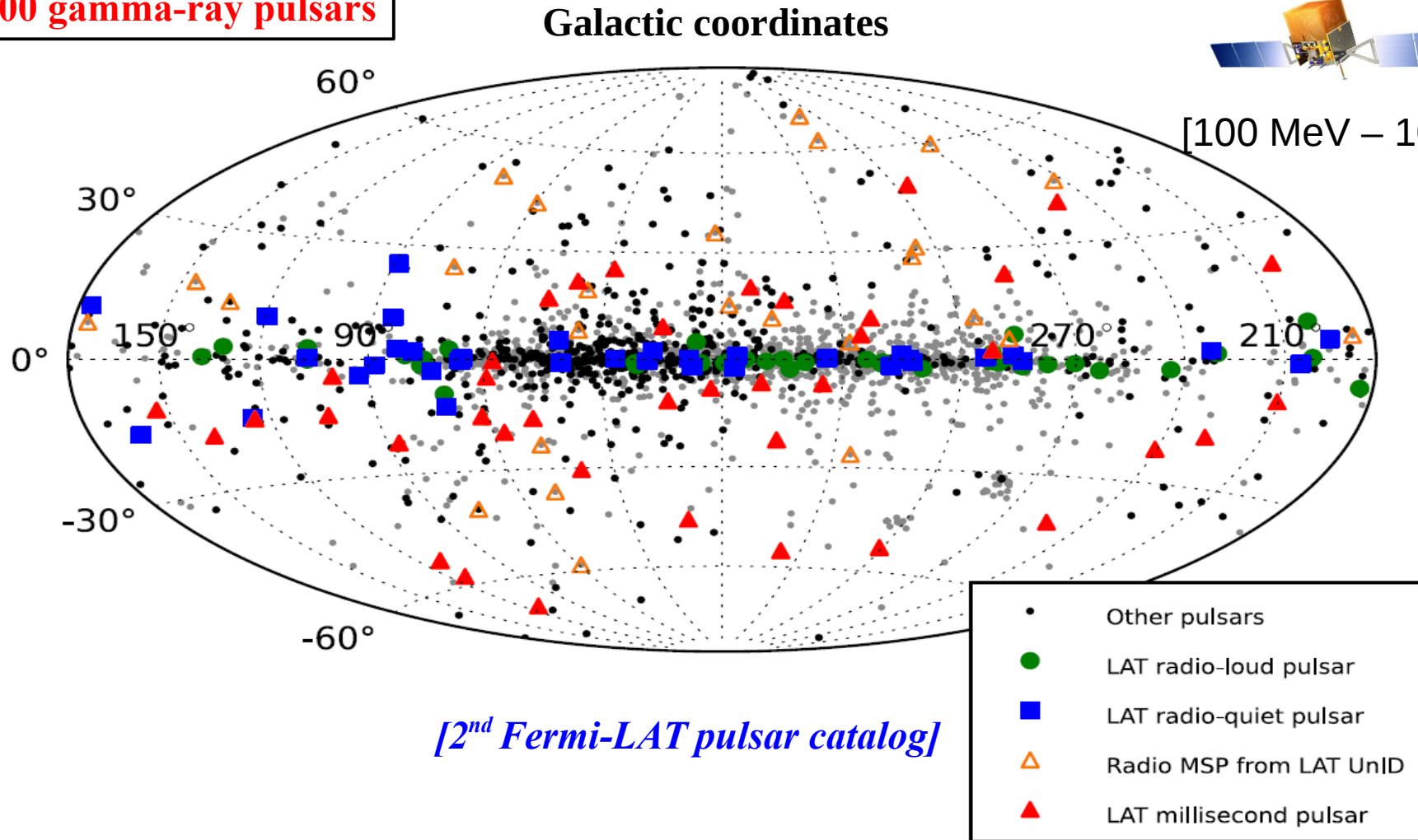
Most Galactic accelerators are pulsars

~ 100 gamma-ray pulsars

Fermi-LAT

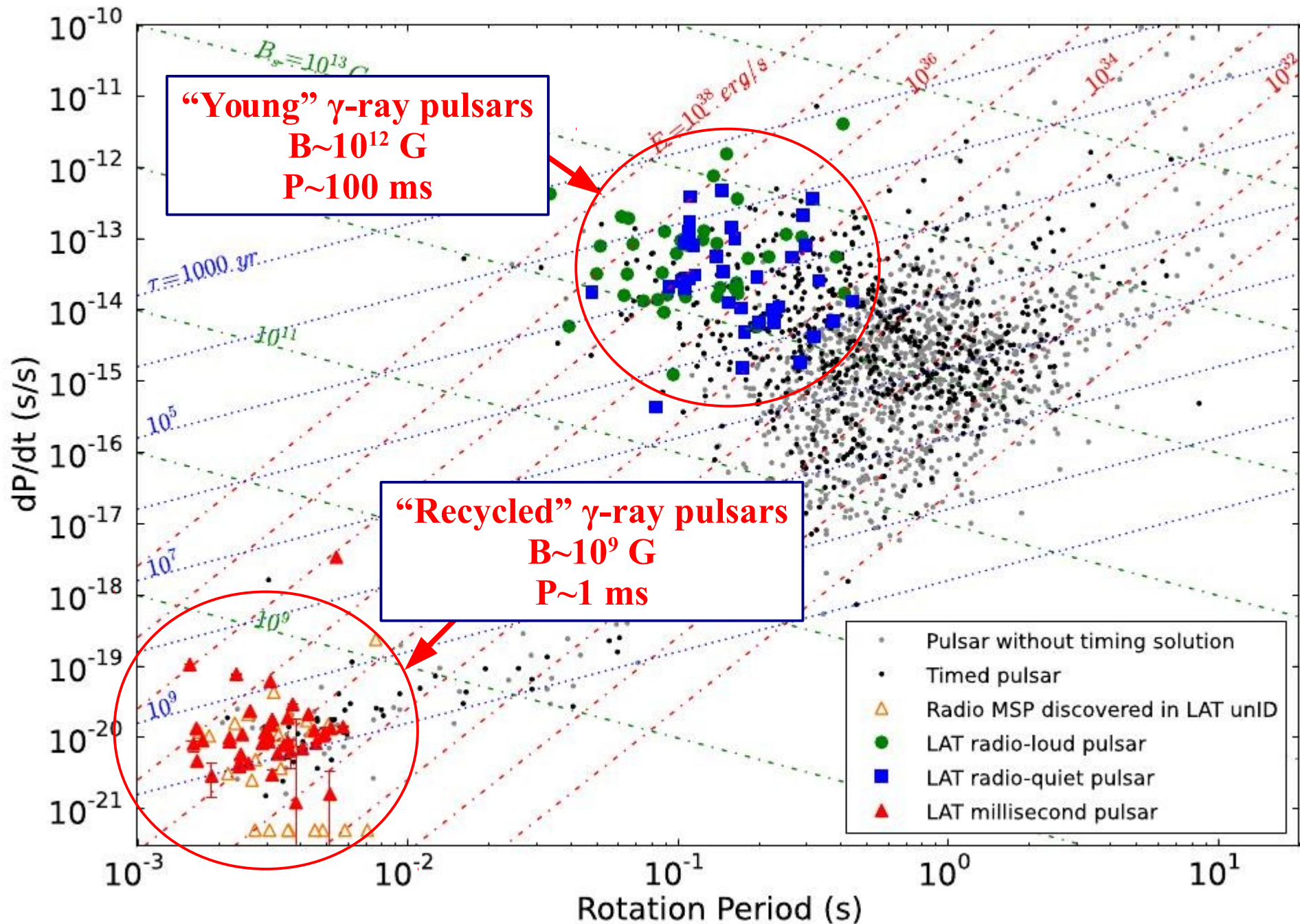


[100 MeV – 100 GeV]

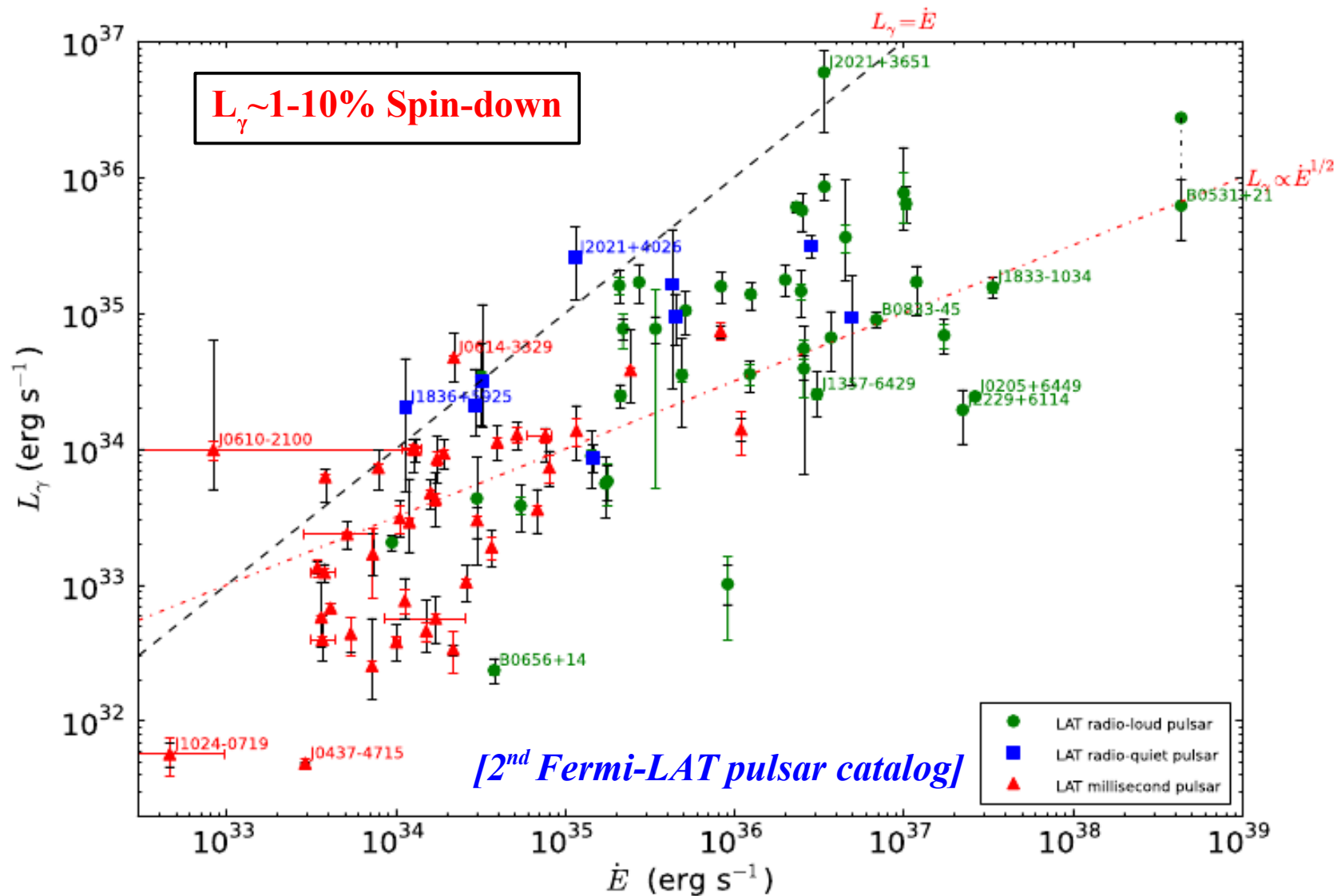


Exquisite gamma-ray data put tight constraints on particle acceleration models

Pulsars emitting gamma rays: **Rotation-powered**



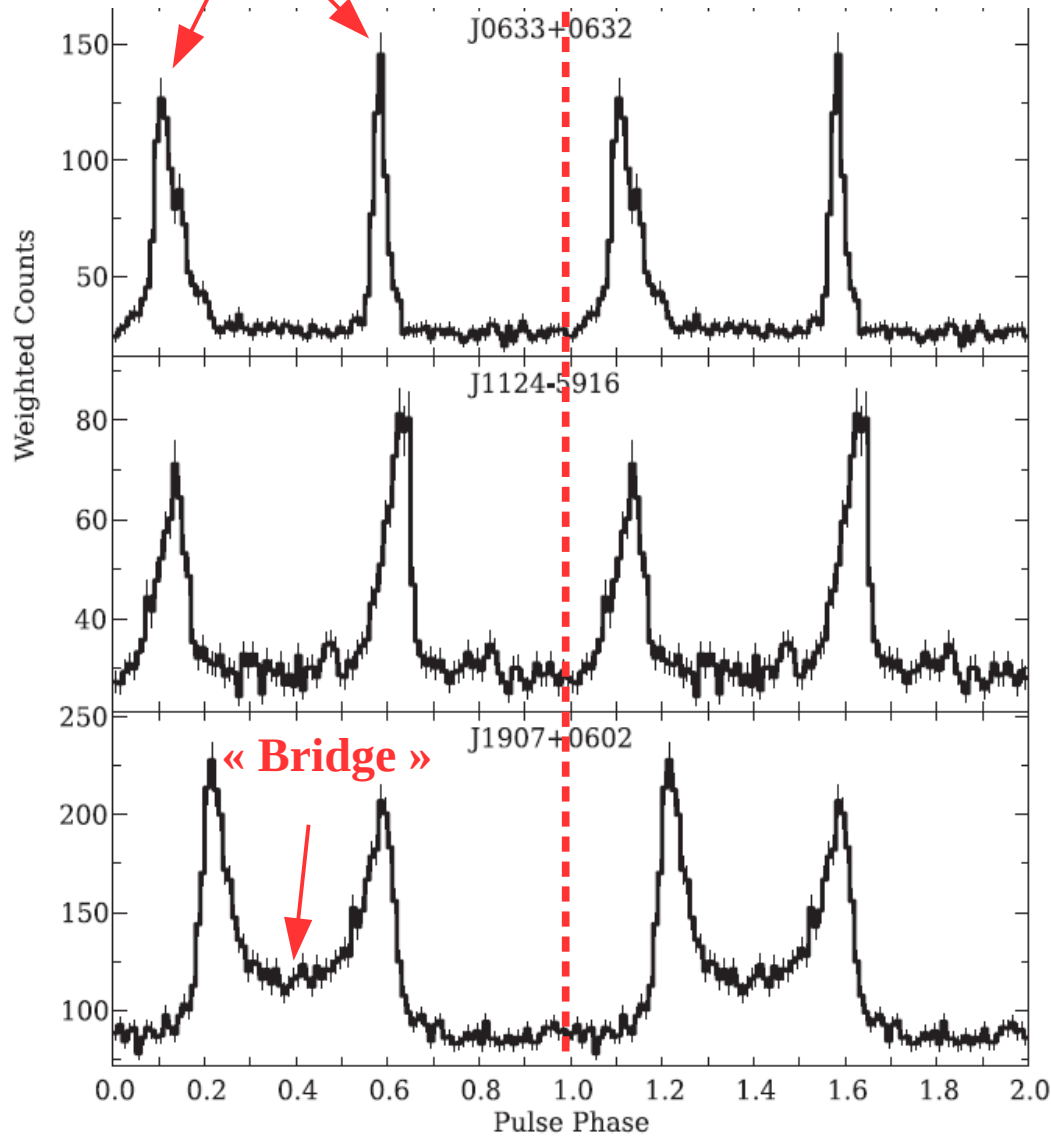
Pulsars are efficient particle accelerators



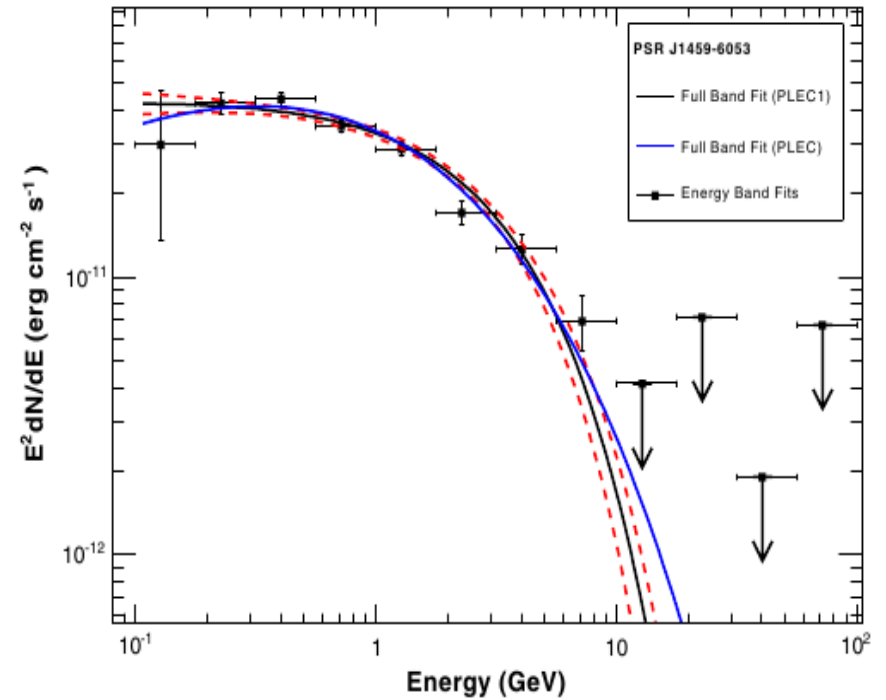
How does the star spin-down?
How is this energy transferred to particles and radiation?

Typical gamma-ray pulsar signal

Two peaks lightcurves



Hard power-law + exponential cut-off



[2nd Fermi-LAT pulsar catalog]

How are particles accelerated and radiate? Origin particle/photon spectra, cut-off?

Some of the big questions

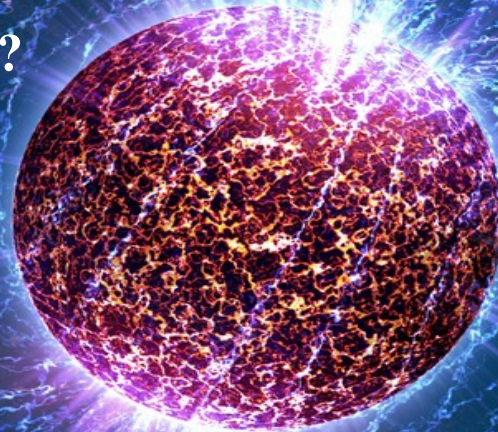
How does the star spin-down?

How is this energy channeled to particles and radiation?

How is the plasma generated?

How are particles accelerated and radiate?

Where is the emission coming from ?



=> To address these questions, we need a model of the magnetosphere!

Elements of a pulsar magnetosphere: **vaccum**

(See review, e.g., [Cerutti & Beloborodov 2016](#))

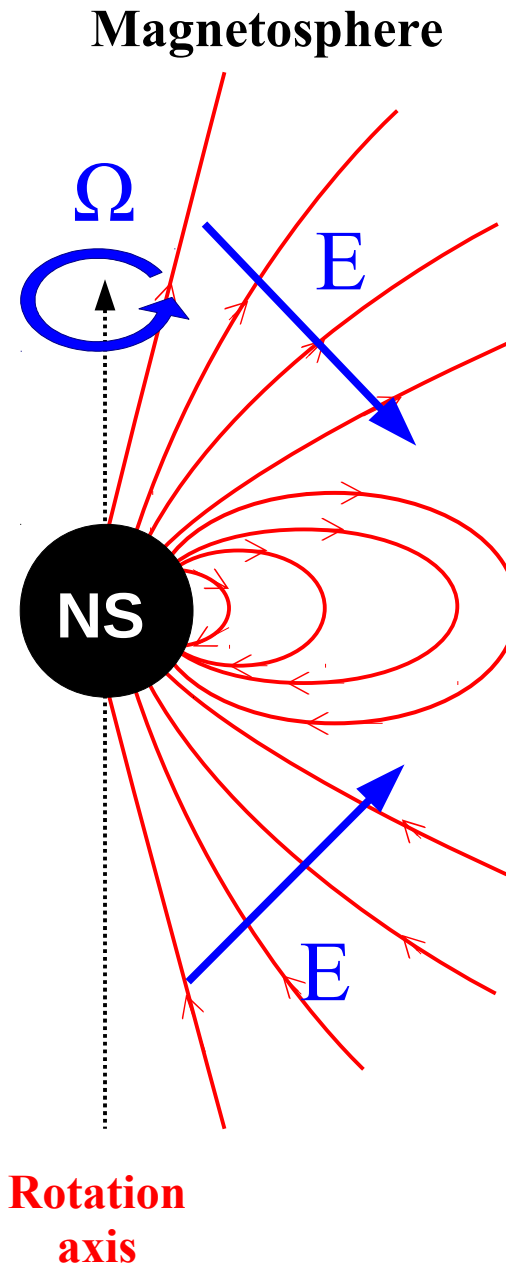
Rotation of the field lines induce electric field :

$$E = \frac{R \Omega B}{c}$$

Potential difference pole/equator :

$$\Delta \Phi = \frac{R^2 \Omega B}{c} \approx 10^{18} \text{ V}$$

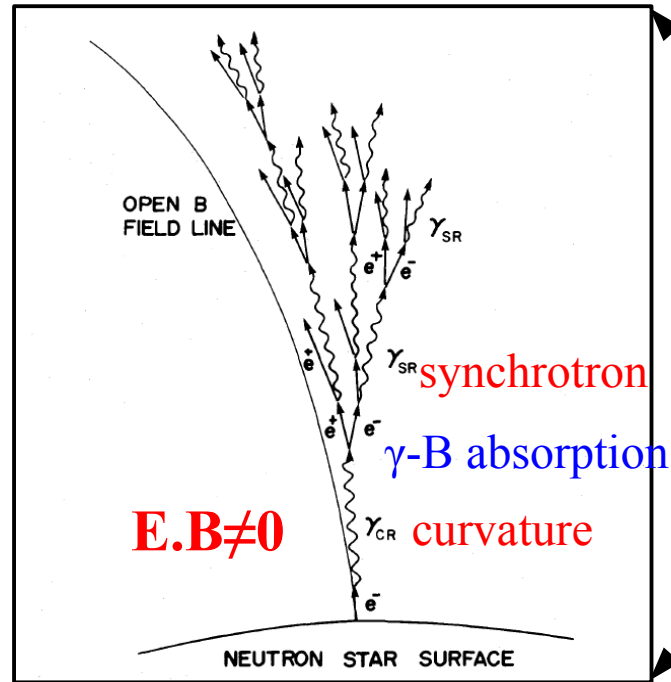
(for a Crab-like pulsar)



Elements of a pulsar magnetosphere: **plasma filled**

Dipole in vacuum is **not** a good model !

Copious pair creation in the polar caps

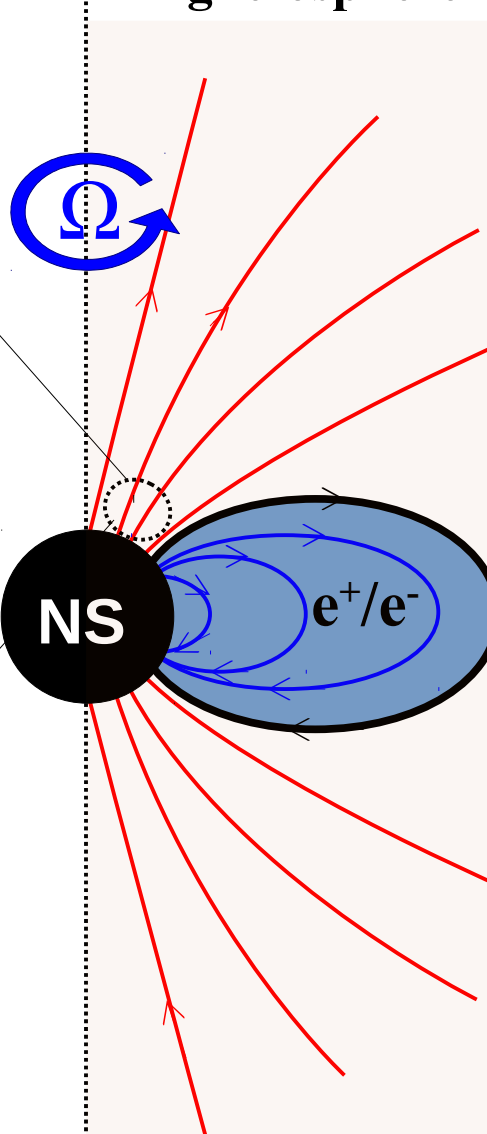


Potential polar cap (Crab):

$$\Delta \Phi_{pc} = \frac{R^3 \Omega^2 B}{c^2} \approx 10^{16} \text{ V}$$

Magnetosphere

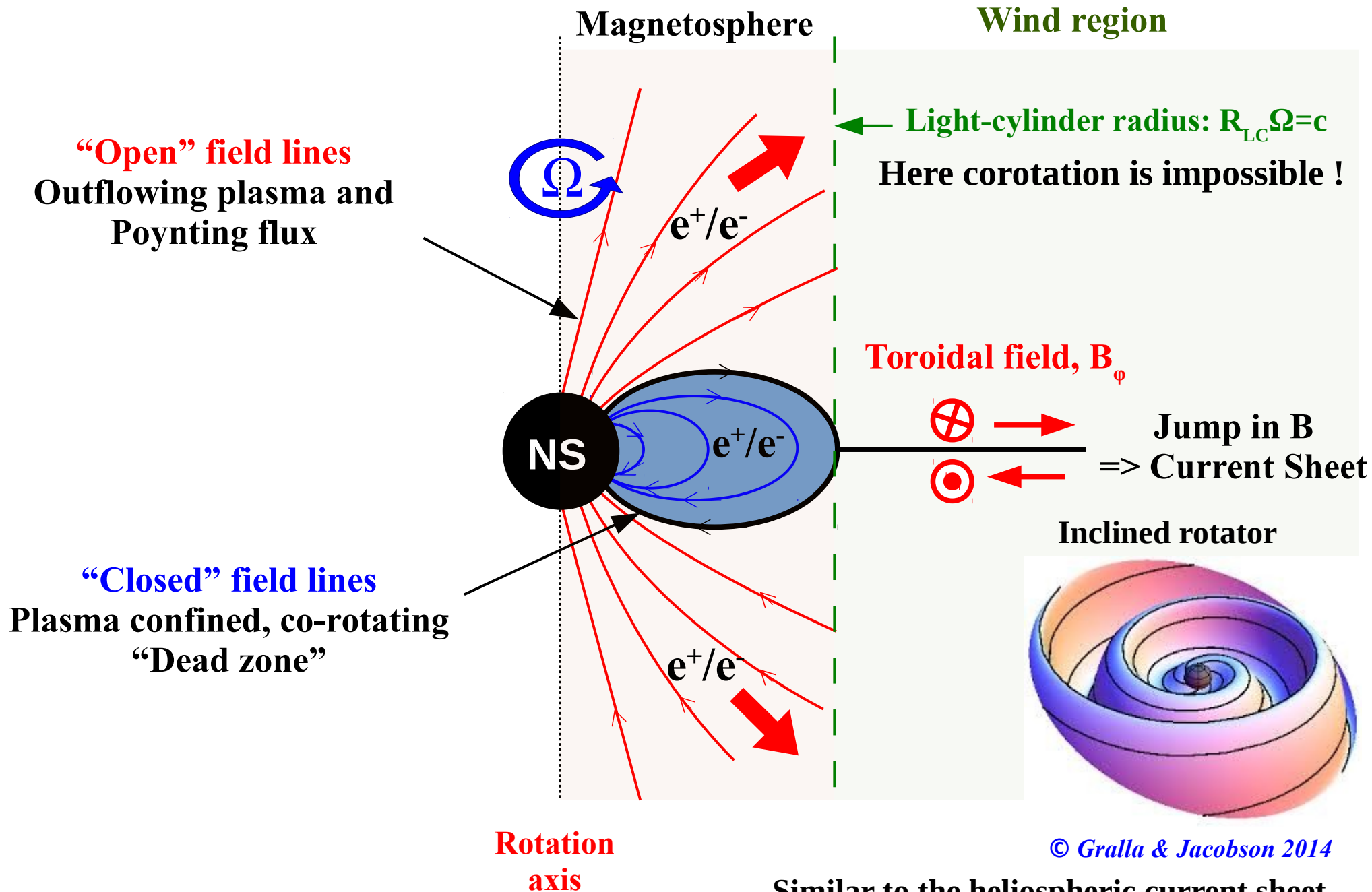
Wind region



← Here corotation is impossible !

Rotation axis

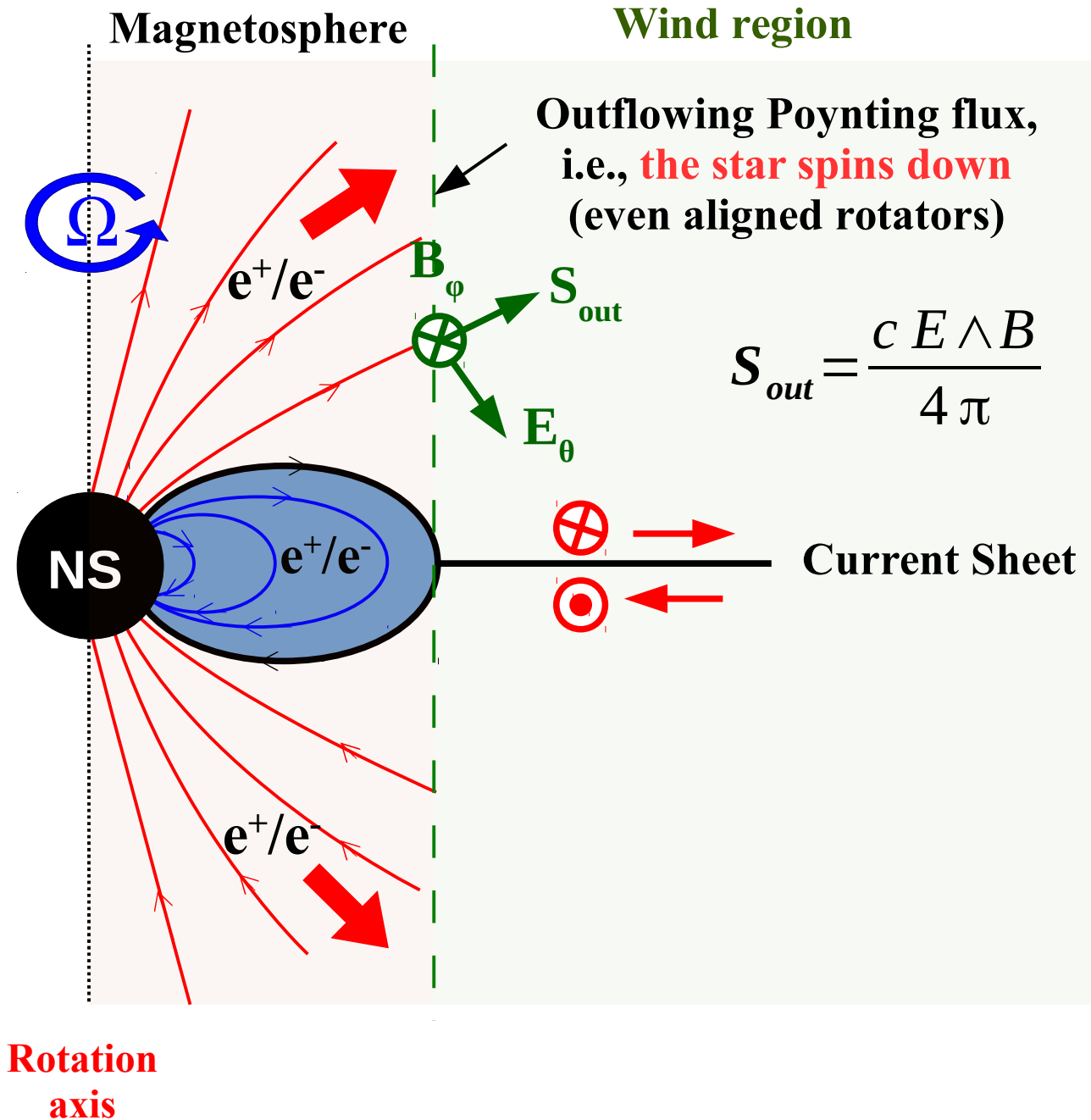
Elements of a pulsar magnetosphere: **plasma filled**



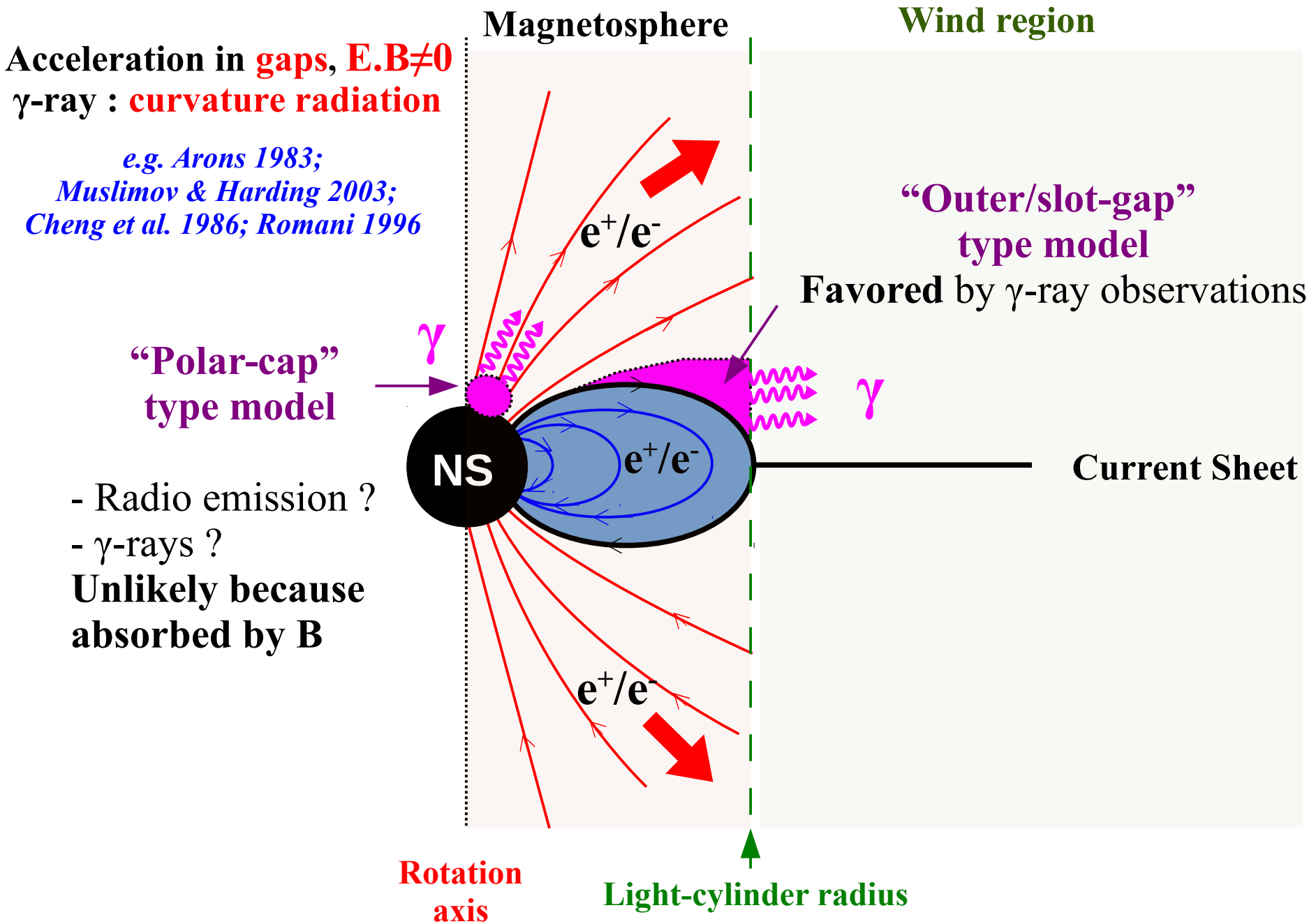
© Gralla & Jacobson 2014

Similar to the heliospheric current sheet.

Elements of a pulsar magnetosphere: **plasma filled**



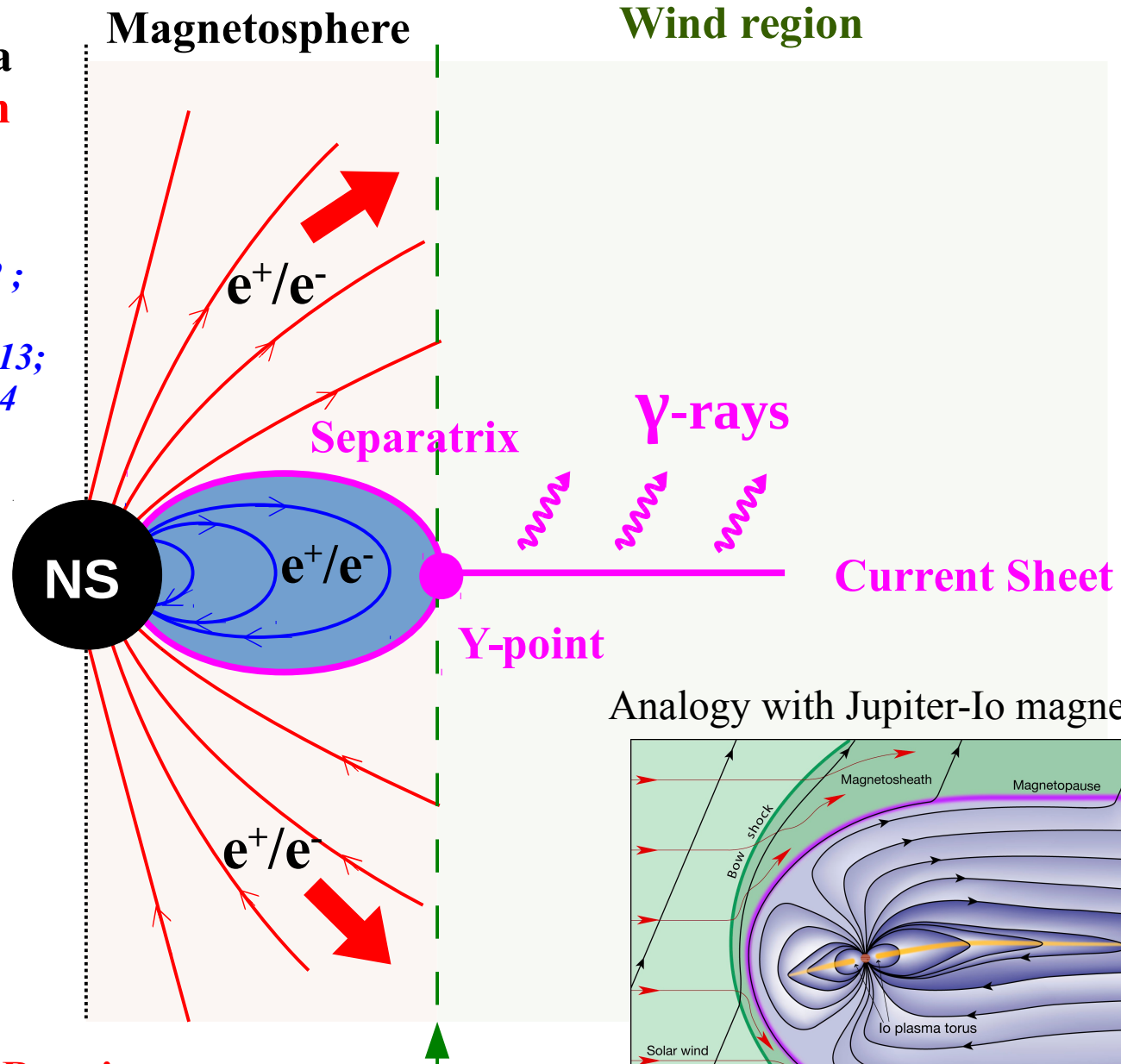
Proposed sites for particle acceleration



Proposed sites for particle acceleration

Particle acceleration via
relativistic reconnection
 γ -ray: **Synchrotron**

*Coroniti 1990 ;
Lyubarskii 1996 ; Kirk+2002 ;
Bai & Spitkovsky 2010 ;
P etri 2012 ; Arka & Dubus 2013 ;
Uzdensky & Spitkovsky 2014
Mochol & P etri 2015*



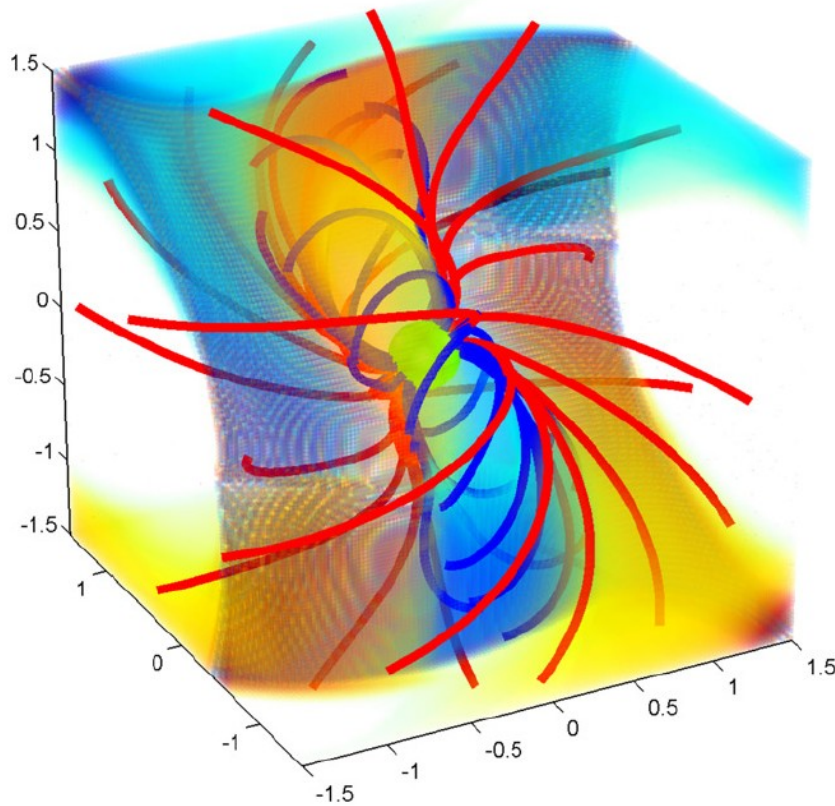
Models dependent on the geometry of the magnetosphere

Insight from the MHD approach

(Force Free / Resistive Force Free / Full MHD)

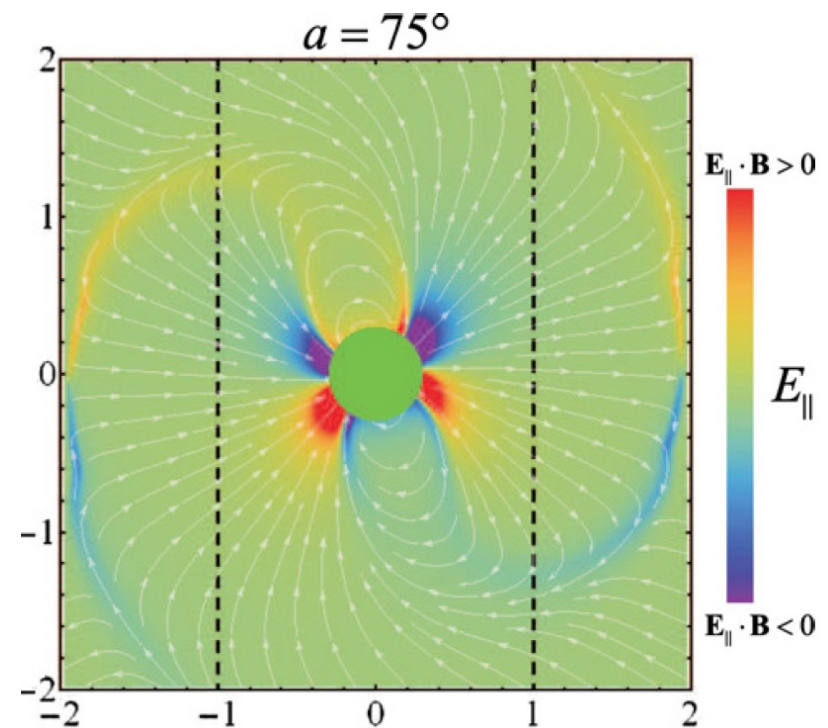
Ideal Force-Free field geometry
with prescribed emitting field lines

Bai & Spitkovsky 2010a,b



Non-ideal Force-Free
with prescribed resistivity

Li et al. 2012; Kalapotharakos et al. 2012, 2014



Favor high-energy emission from the **outer magnetosphere + current sheet**

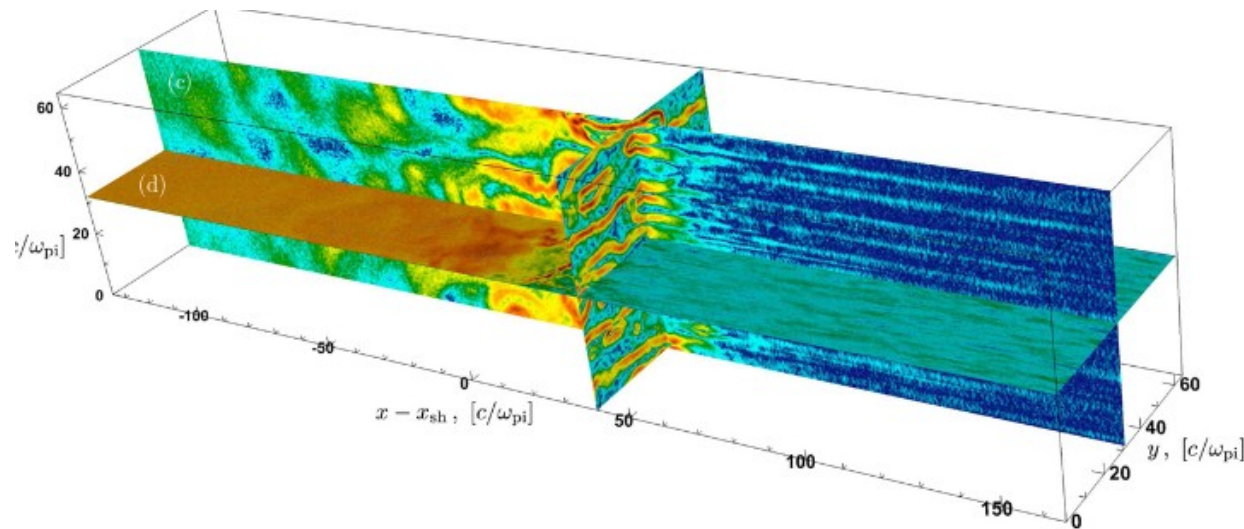
Ad-hoc accelerating/radiating zones, large uncertainties \rightarrow Need for self-consistent approach

B. Cerutti

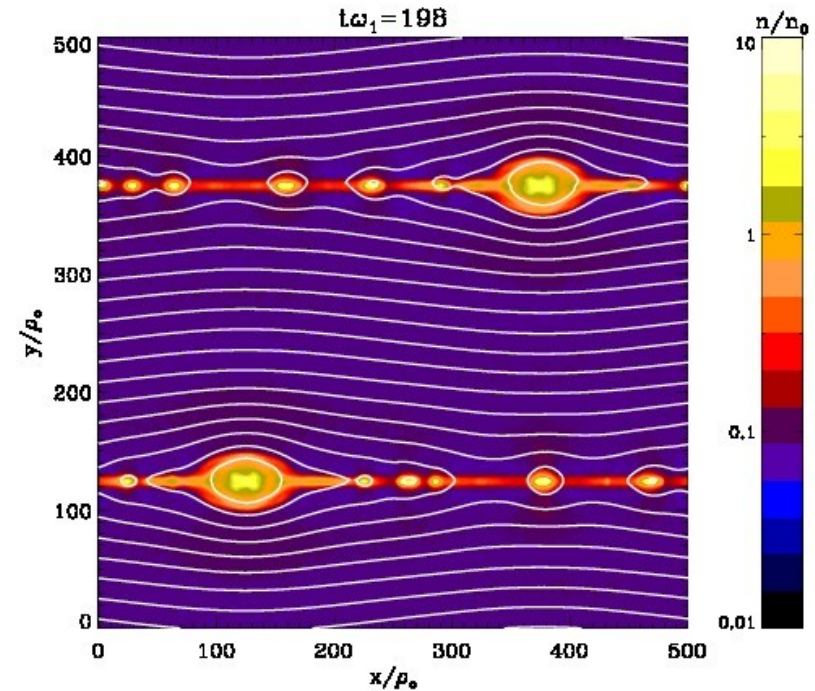
Particle-in-Cell simulations!

Astrophysical applications of the PIC methods

Particle acceleration in **collisionless shocks** and **reconnection**



[Sironi et al. 2013]



[Cerutti et al. 2013]

This method is always applied to a **microscopic part** of an astrophysical system due to the **huge scale separation**.

In pulsars, we need to **solve the problem globally!** Such simulations were already performed by:

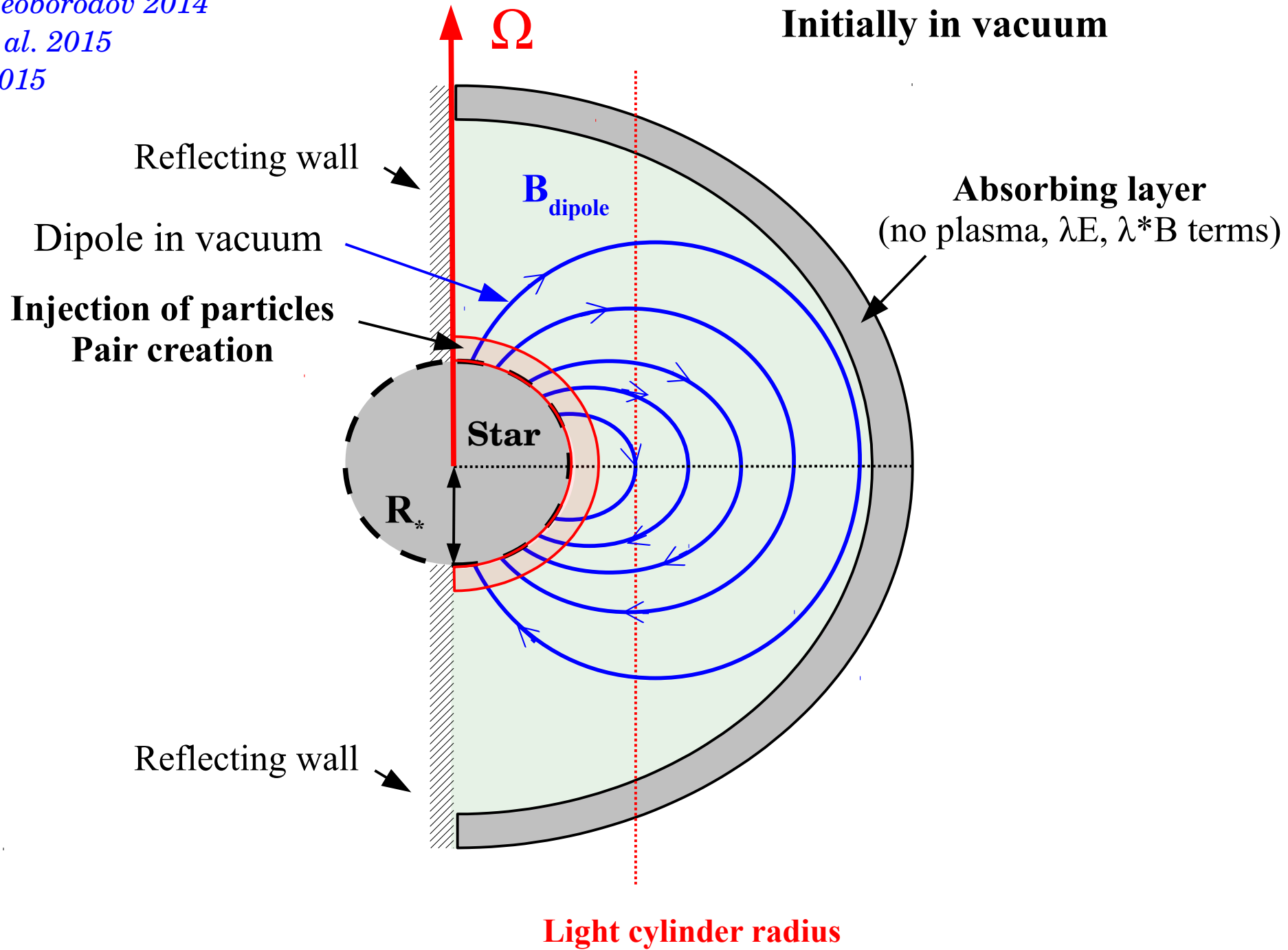
Philippov et al. 2014, 2015, Chen & Beloborodov 2014, Cerutti et al. 2015 & 2016, Belyaev 2015

The numerical setup: an aligned rotator (2D)

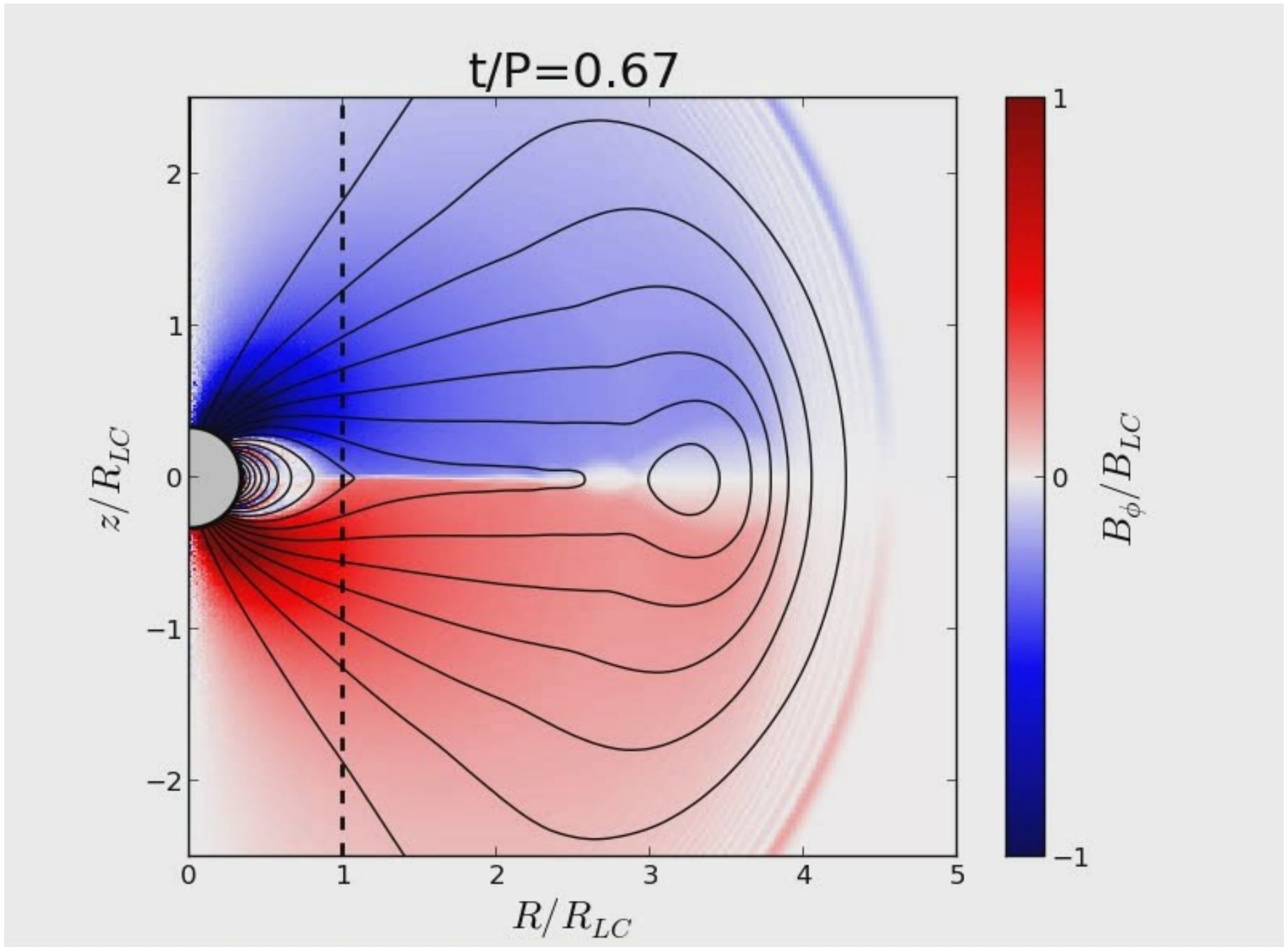
Chen & Beoborodov 2014

Cerutti et al. 2015

Belyaev 2015

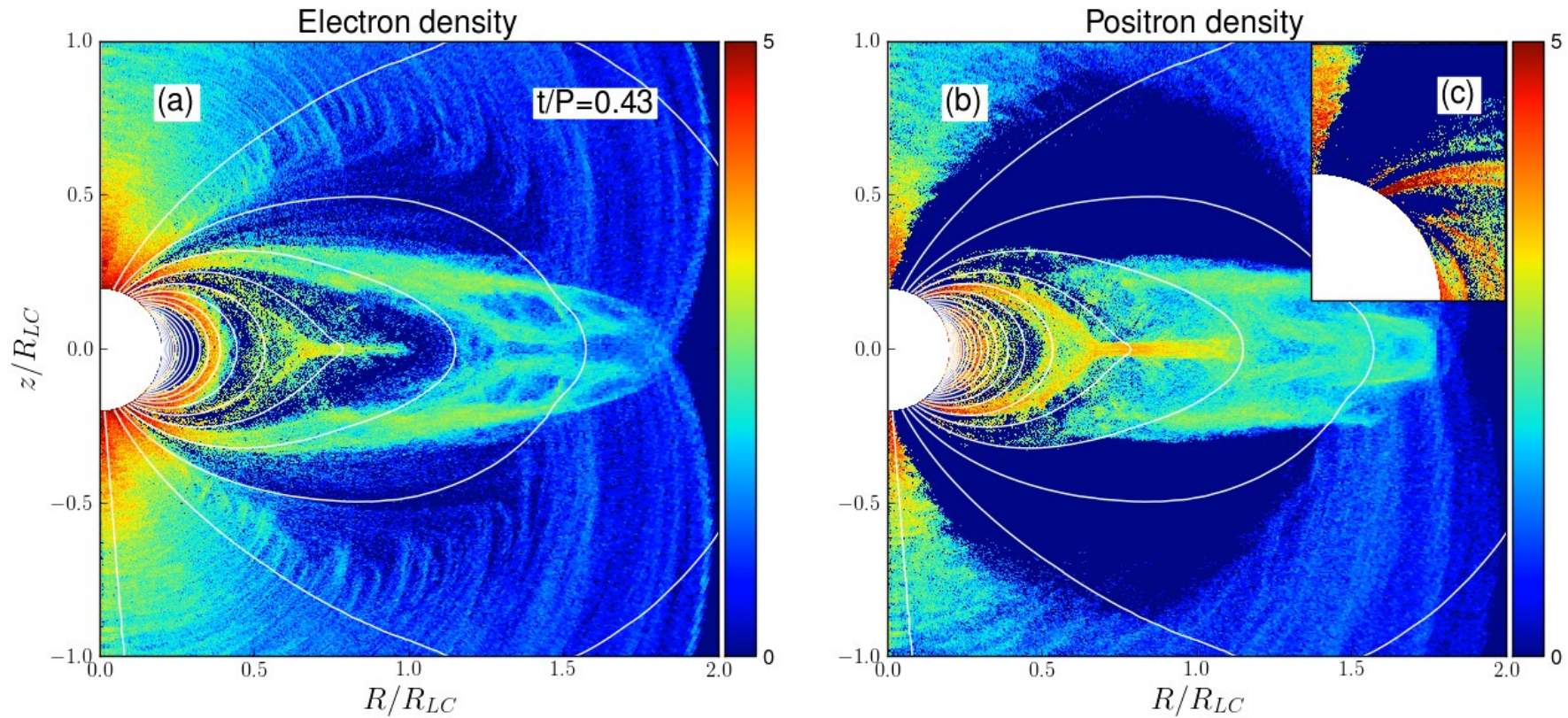


Toroidal magnetic field



Pair creation and filling of the magnetosphere

Pair creation at the **polar caps** (γB) and within the **current sheet** ($\gamma\gamma$)



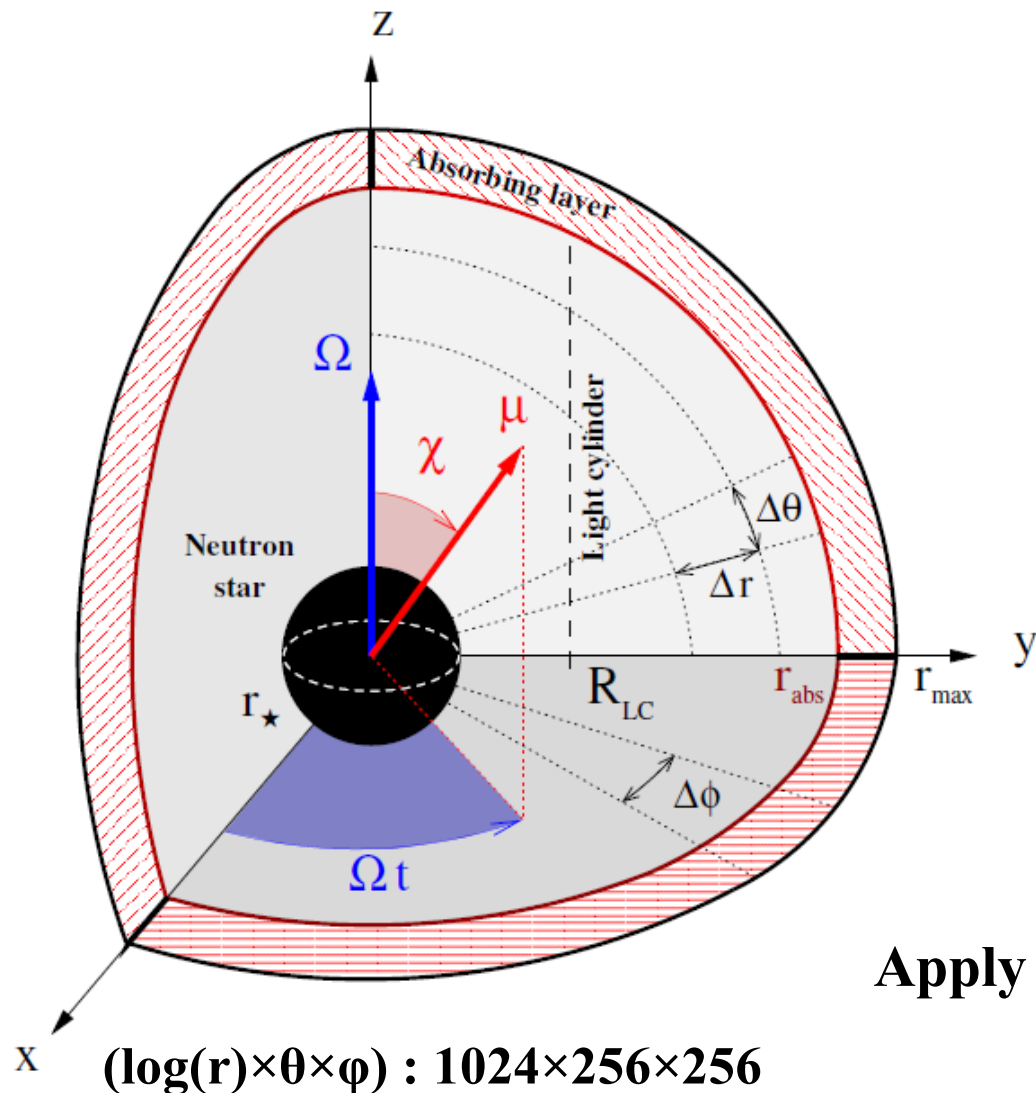
Courtesy of Sasha Philippov

[Philippov et al. 2015b]

Global 3D spherical PIC with radiation reaction force

Zeltron code : <http://benoit.cerutti.free.fr/Zeltron/>

Assumption : Large plasma supply provided by the star surface = **Efficient pair creation**



Radiation reaction force

$$\frac{d(\gamma m_e \mathbf{v})}{dt} = q (\mathbf{E} + \boldsymbol{\beta} \times \mathbf{B}) + \mathbf{g},$$

Emitted radiation spectra :

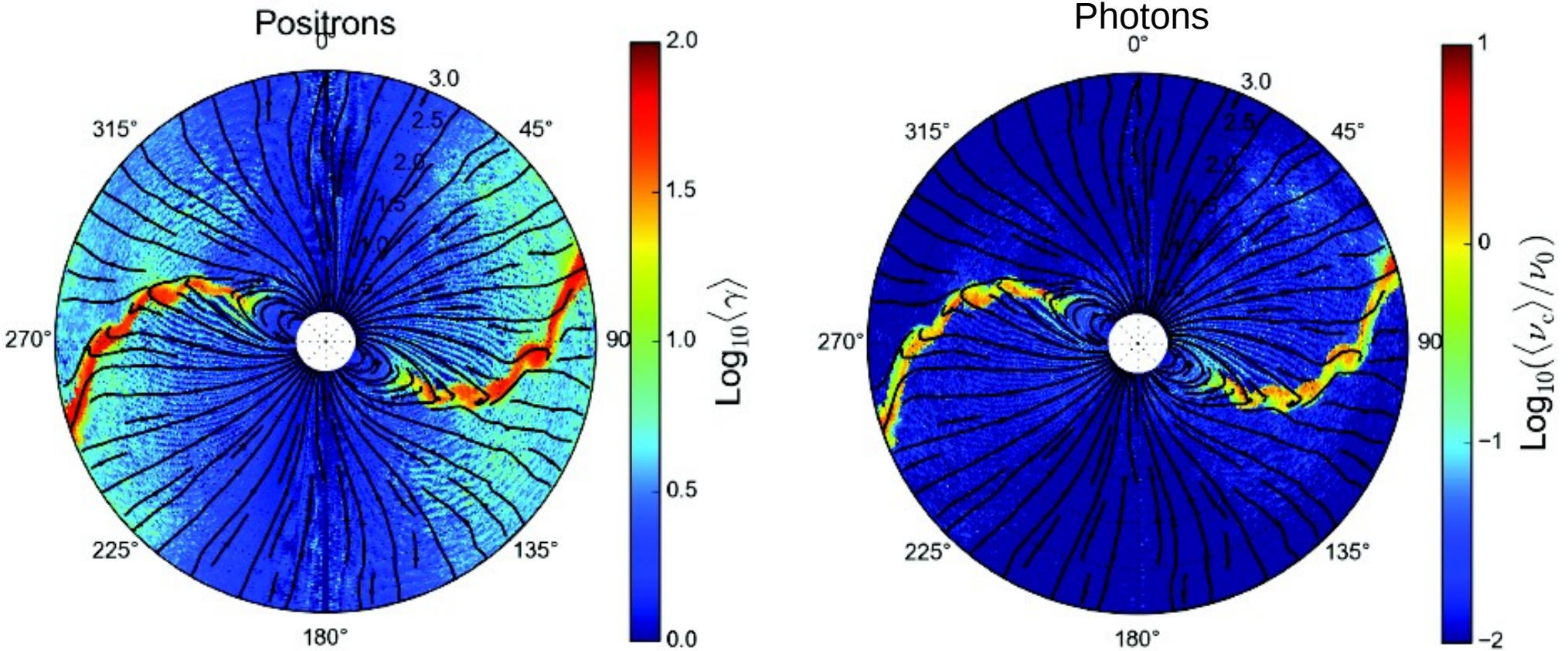
$$F_\nu(\nu) = \frac{\sqrt{3} e^3 \tilde{B}_\perp}{m_e c^2} \left(\frac{\nu}{\nu_c} \right) \int_{\nu/\nu_c}^{+\infty} K_{5/3}(x) dx,$$

$$\tilde{B}_\perp = \sqrt{(\mathbf{E} + \boldsymbol{\beta} \times \mathbf{B})^2 - (\boldsymbol{\beta} \cdot \mathbf{E})^2},$$

Apply for **synchrotron** and **curvature** radiation

Particle / radiation mean energy ($\chi=30^\circ$)

Cerutti et al. 2016



Particle acceleration via relativistic *reconnection* in the *current sheet*
High-energy radiation is *synchrotron radiation*

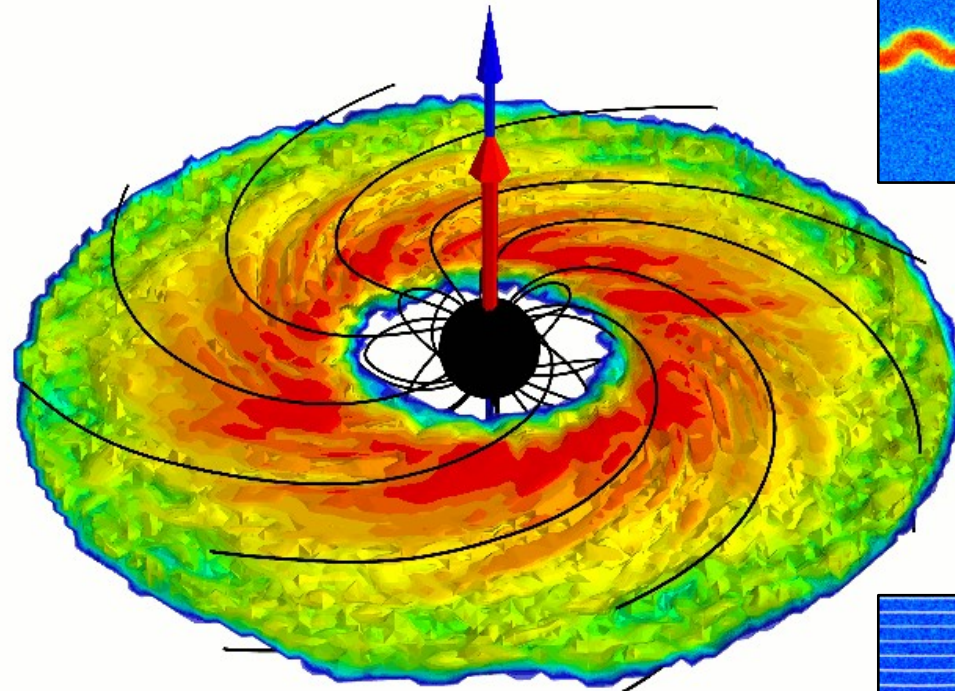
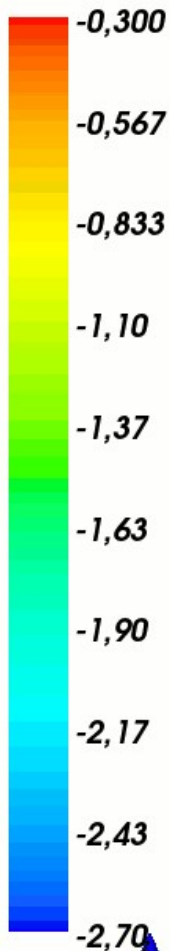
Particle energy in the sheet given by :

$$\sigma_{LC} = \frac{B_{LC}^2}{4\pi\Gamma n_{LC} m_e c^2} \approx 50 \quad (\text{here})$$

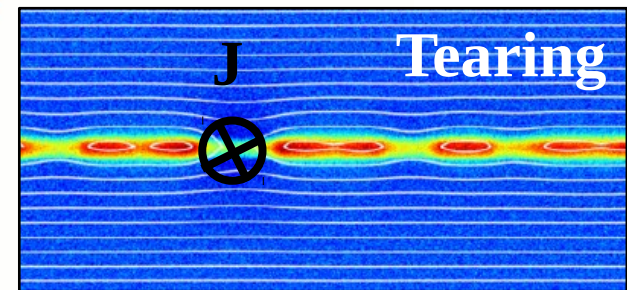
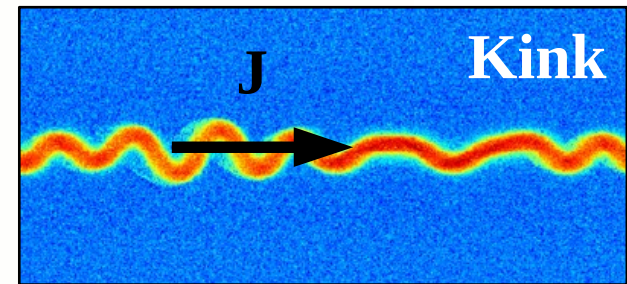
High-energy radiation flux ($v > v_0$, $\chi = 0^\circ$)

$i=0$ - Phase=0.00 - Positrons -

Log(Flux)



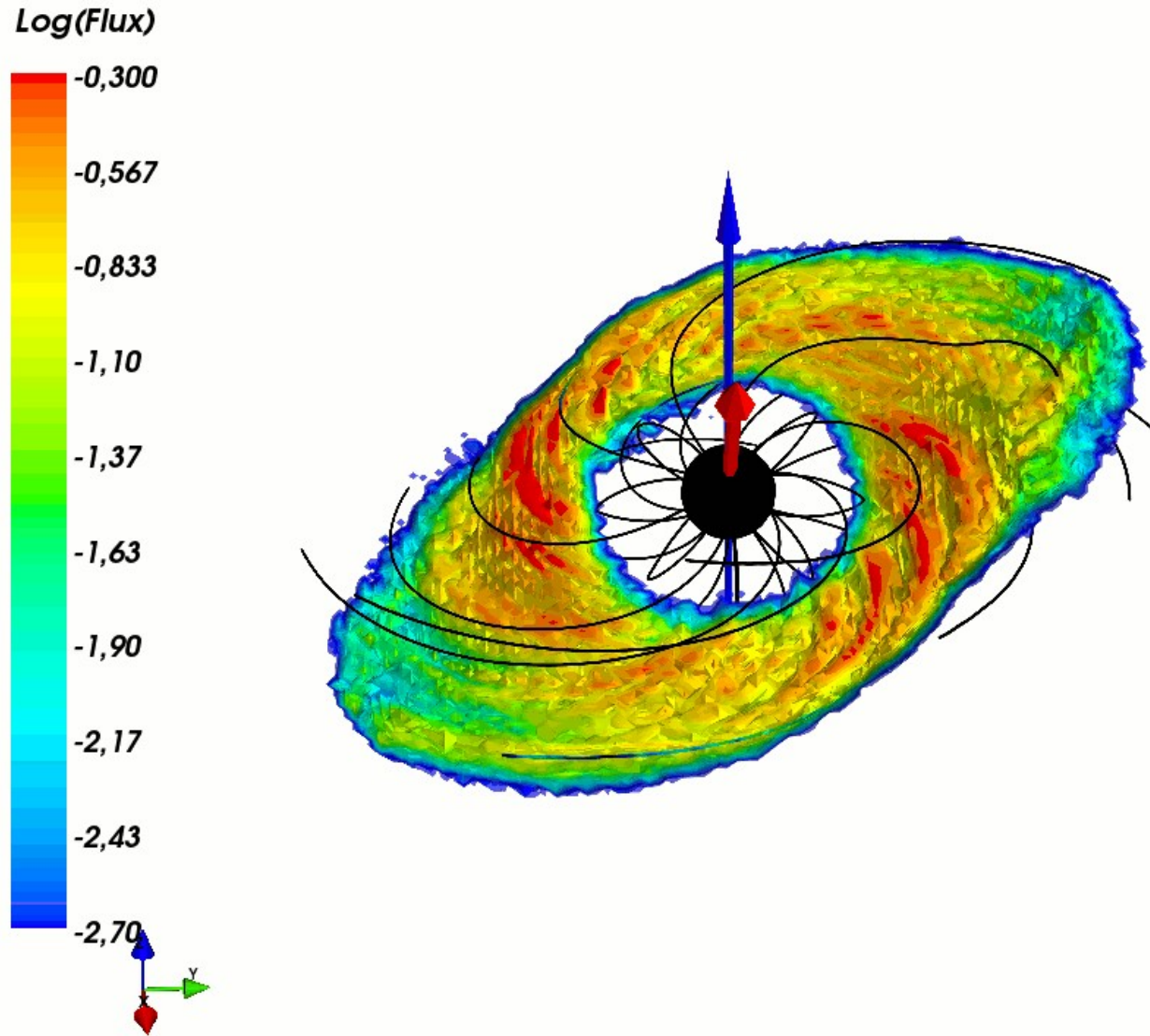
(from Local reconnection simulations)



Presence of spatial irregularities due to **kinetic instabilities** in the sheet
(e.g., kink and tearing modes)

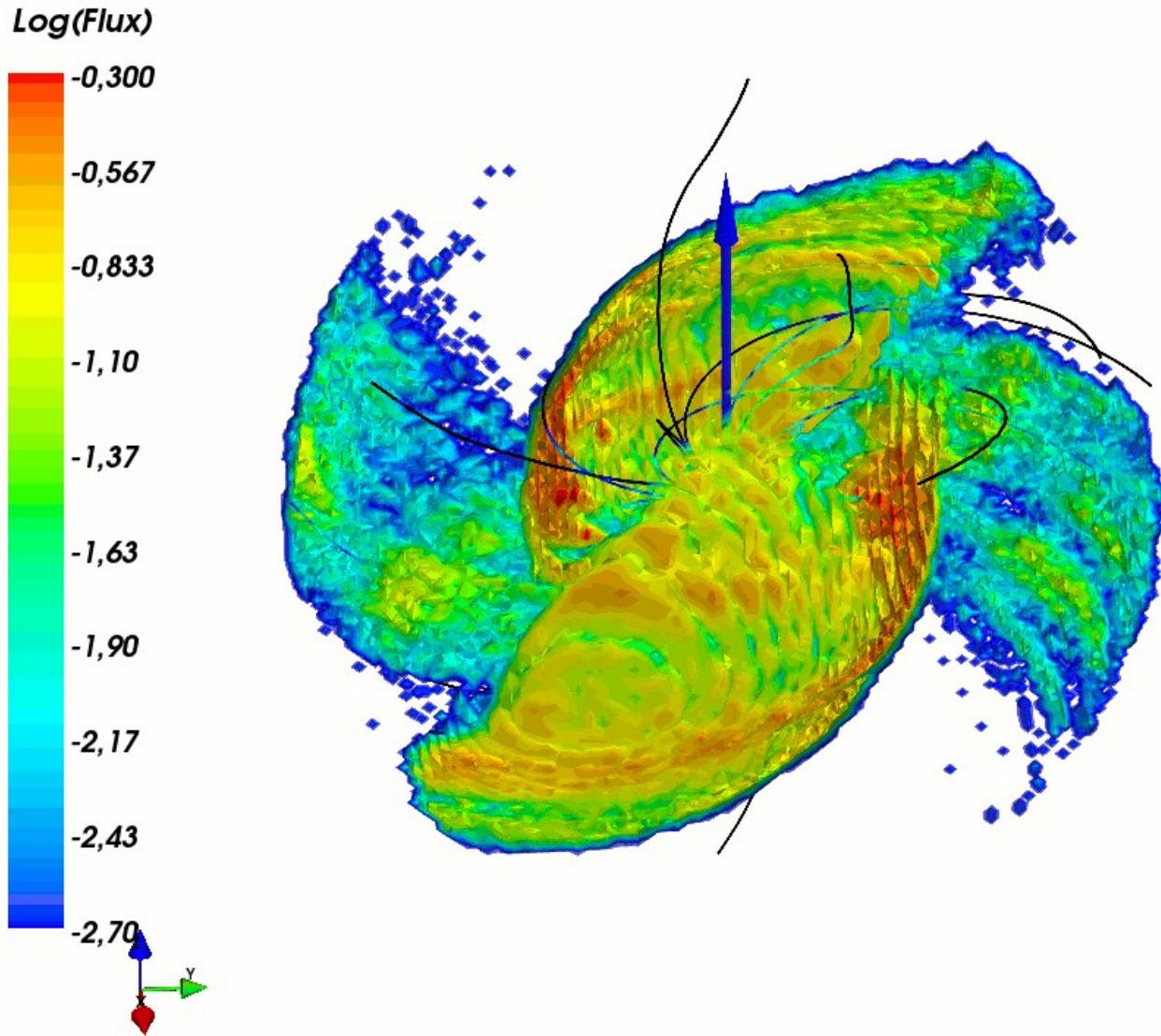
High-energy radiation flux ($\nu > \nu_0$, $\chi = 30^\circ$)

$i=30$ - Phase=0.00 - Positrons -

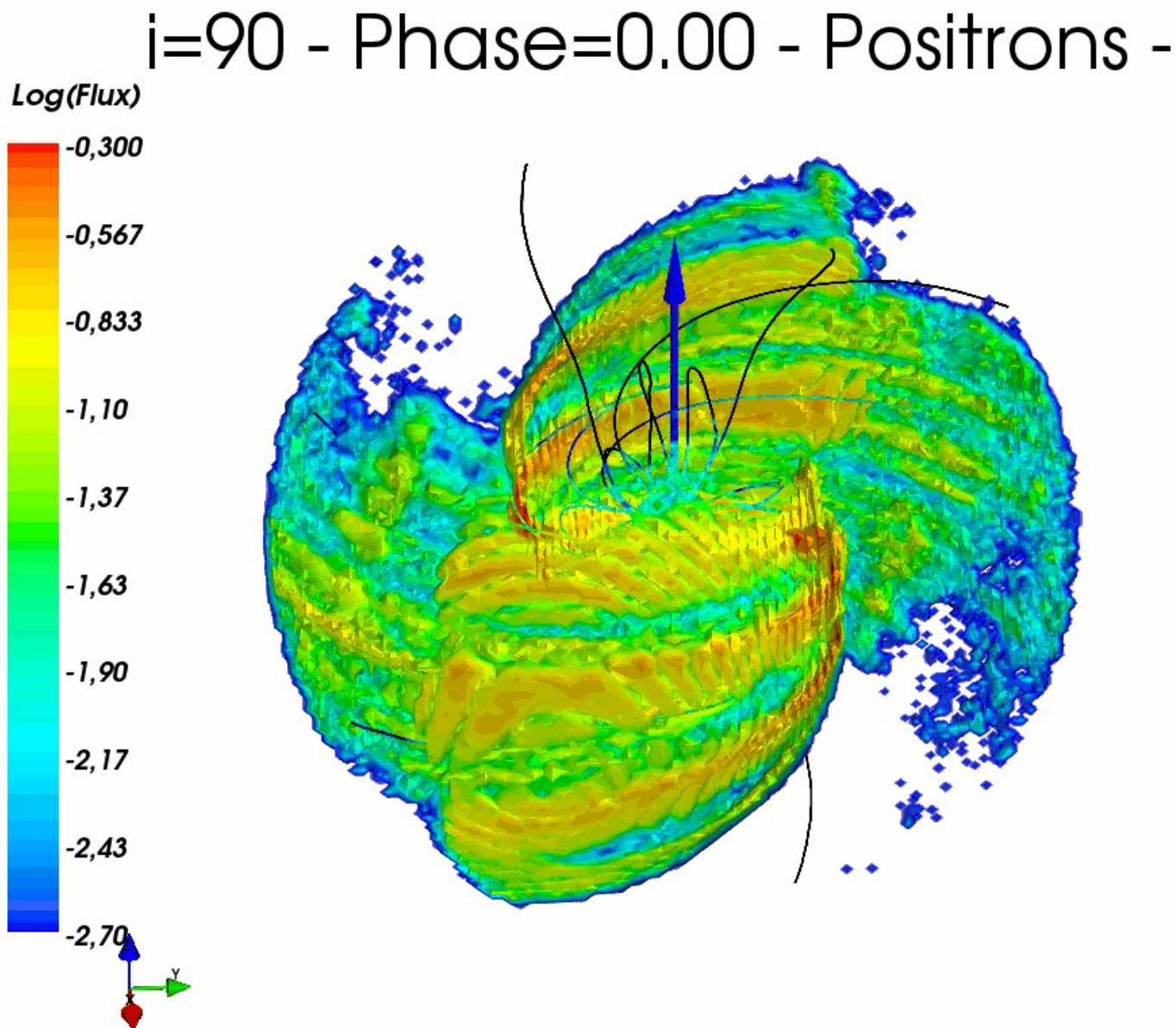


High-energy radiation flux ($v > v_0$, $\chi = 60^\circ$)

$i=60$ - Phase=0.00 - Positrons -



High-energy radiation flux ($\nu > \nu_0$, $\chi = 90^\circ$)



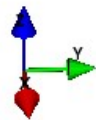
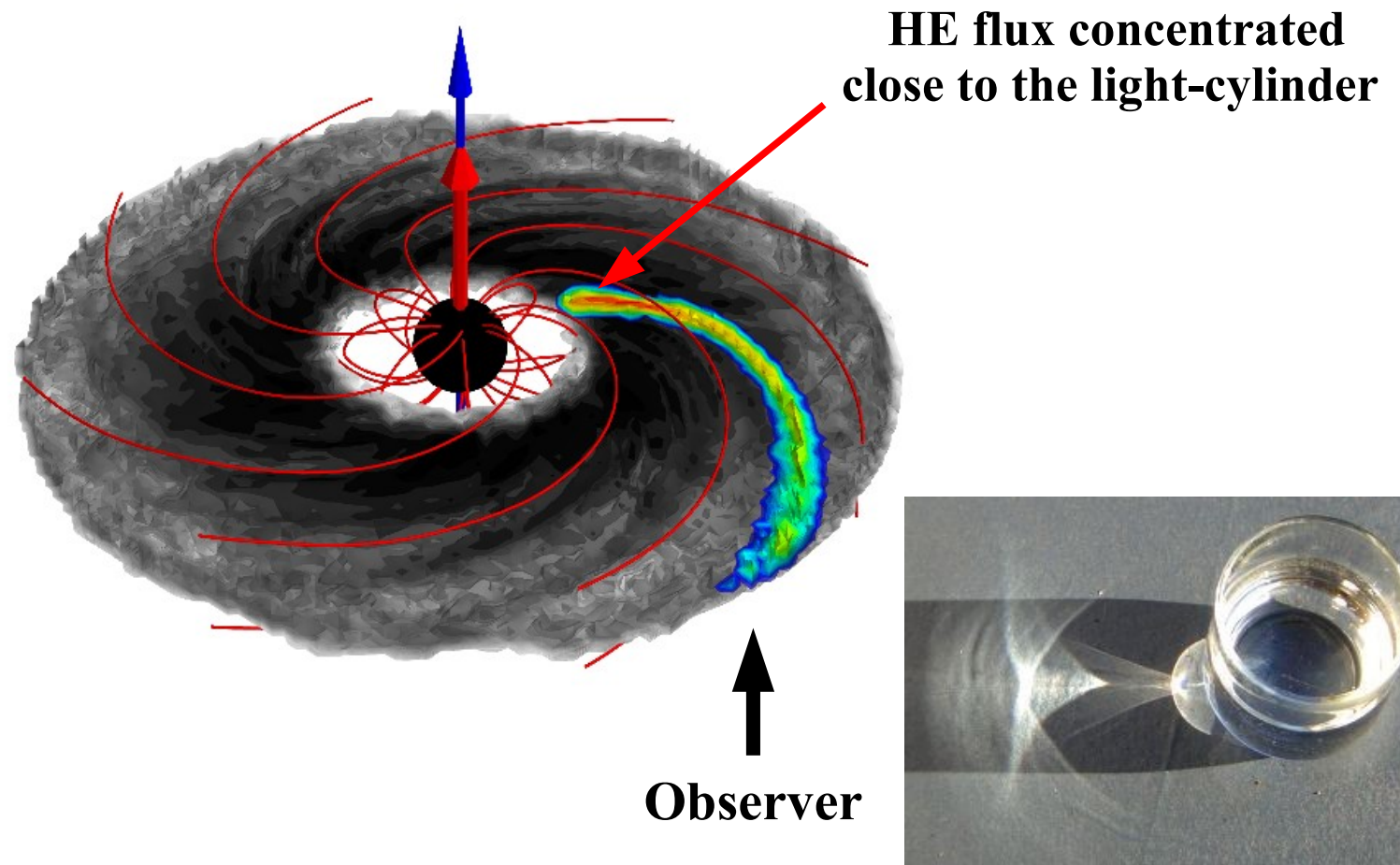
Even for the orthogonal rotator, high-energy photons are **concentrated within the equatorial regions** where most of the spin-down is dissipated.

Observed high-energy radiation flux ($\nu > \nu_0$, $\chi = 0^\circ$)

Gray : Total flux (all directions)

Color : Observed flux

$i=0$ - Phase=0.00 - Positrons -



Spatial **extension** of the observed emission in the sheet

=> Formation of a **caustic**

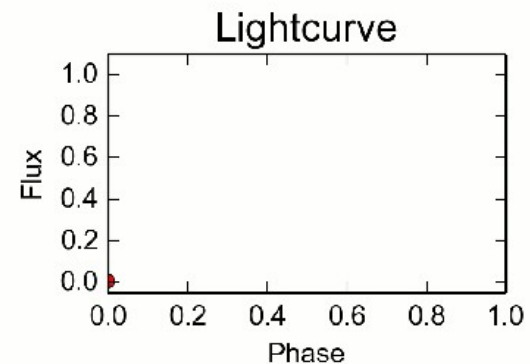
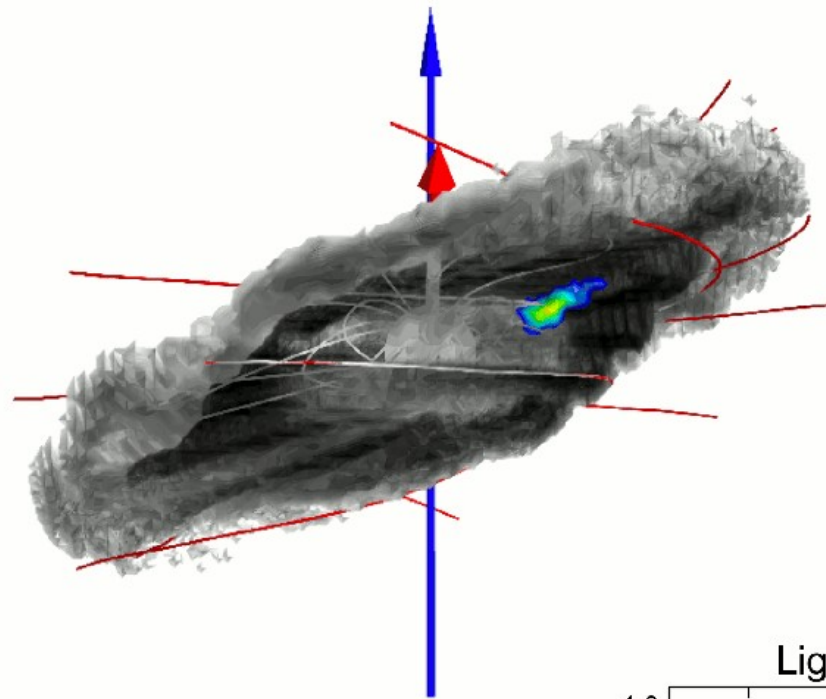
Observed high-energy radiation flux ($\nu > \nu_0$, $\chi = 30^\circ$)

Gray : Total flux (all directions)

Color : Observed flux

Light curve **shaped by the geometry** of the current sheet

$i=30$ - Phase=0.00 - Positrons -



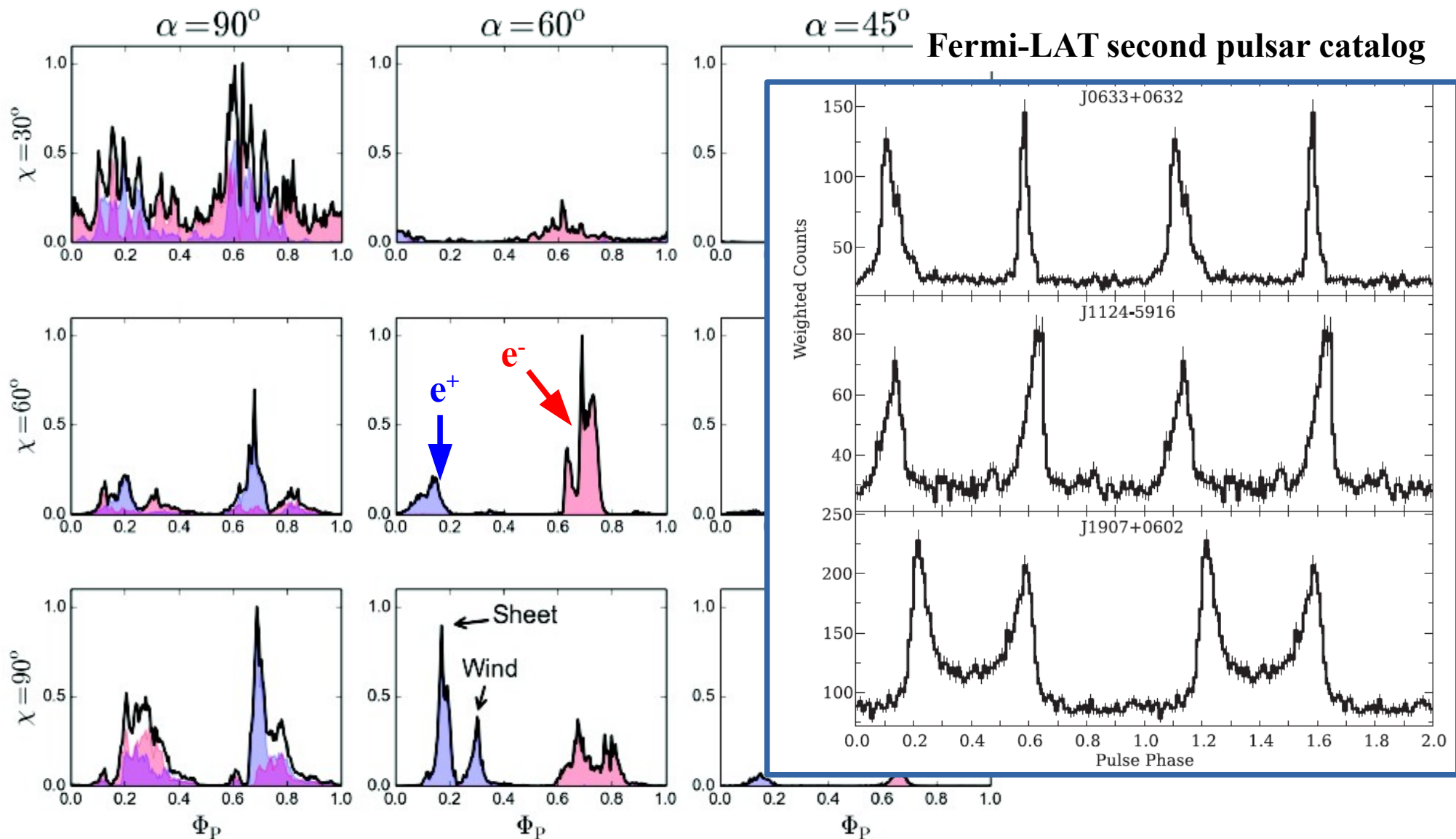
Two-peaked lightcurves are very generic

One peak per crossing of the current sheet

Blue : Positronic emission

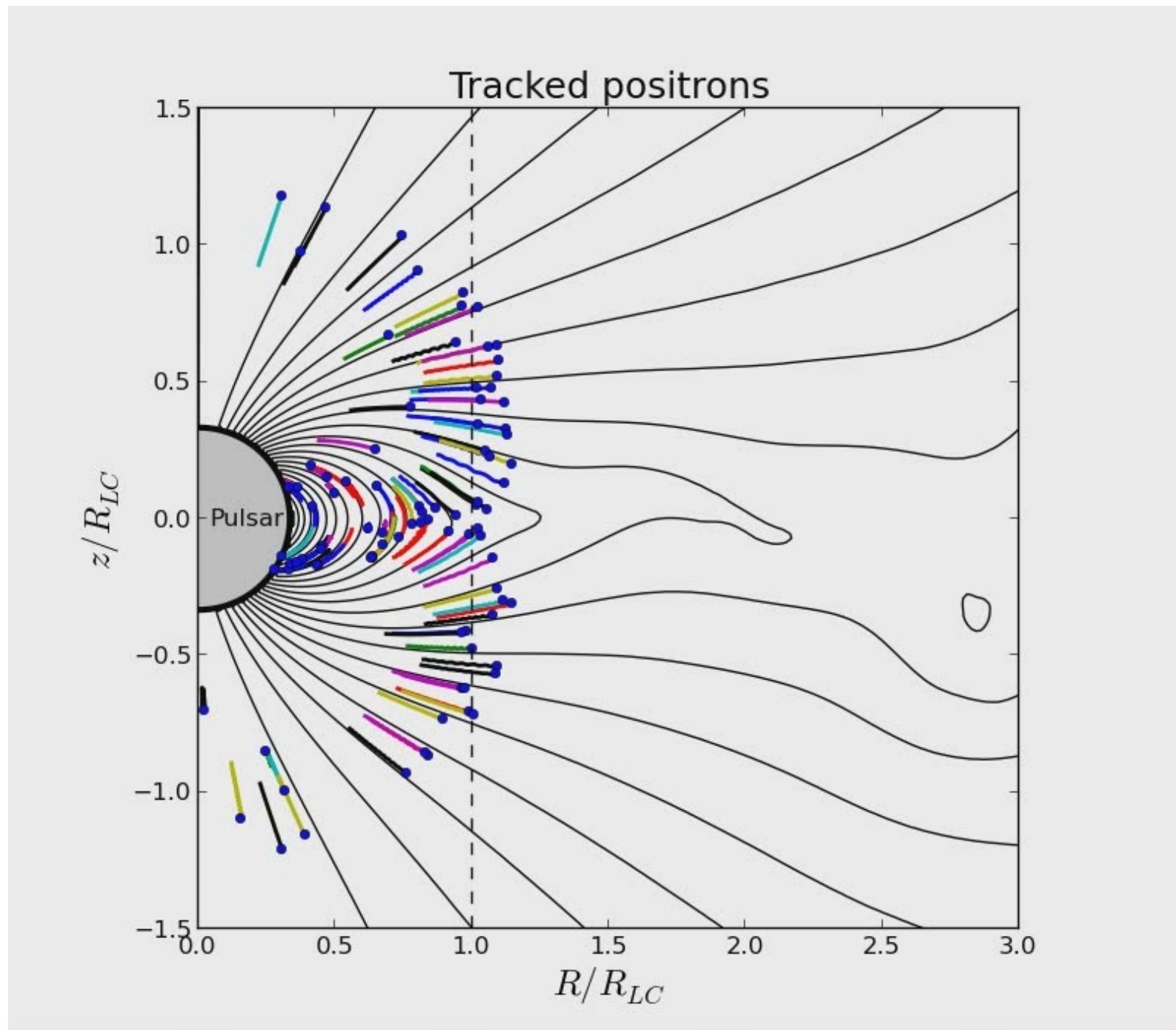
Red : Electronic emission

Viewing angle



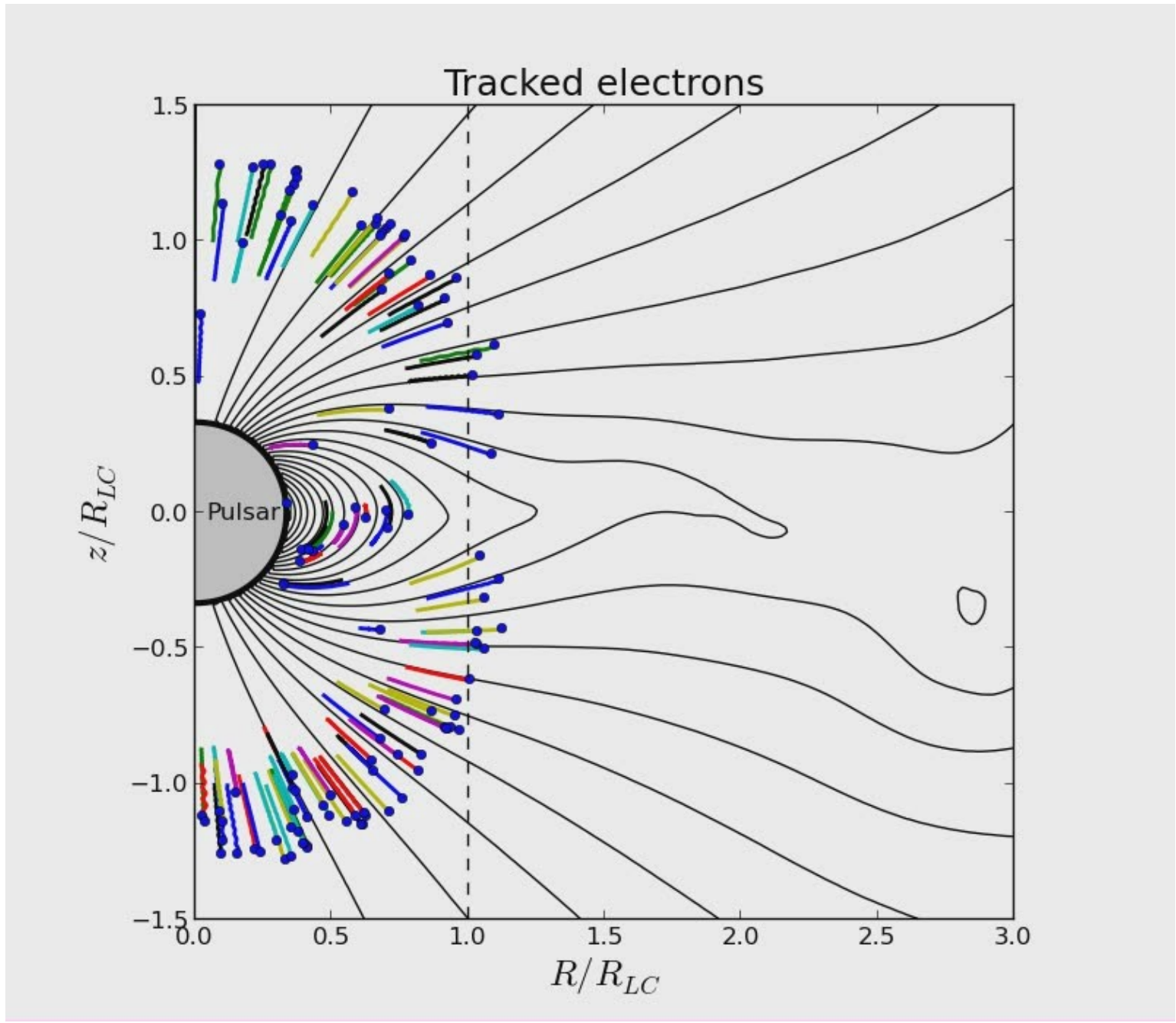
Particle acceleration and origin of the e^+/e^- asymmetry

2D



Particle acceleration and origin of the e^+/e^- asymmetry

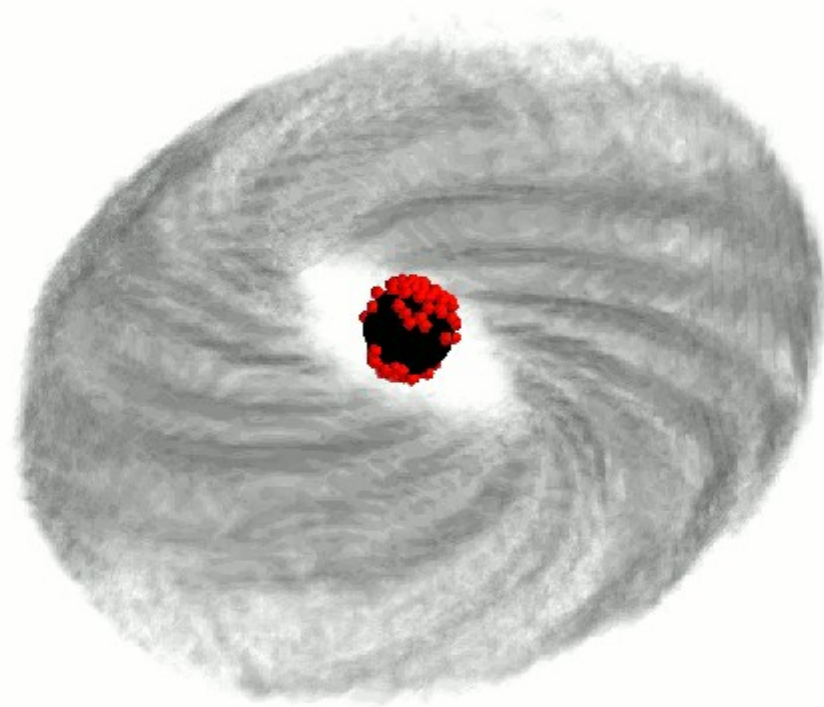
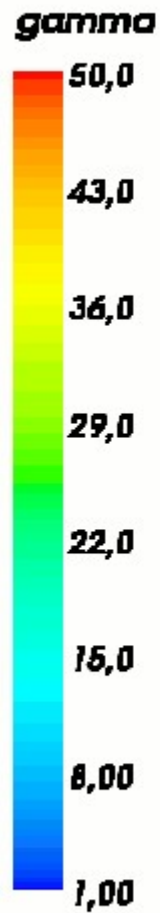
2D



Particle acceleration and origin of the e^+/e^- asymmetry

In the co-rotating frame

Tracked positrons

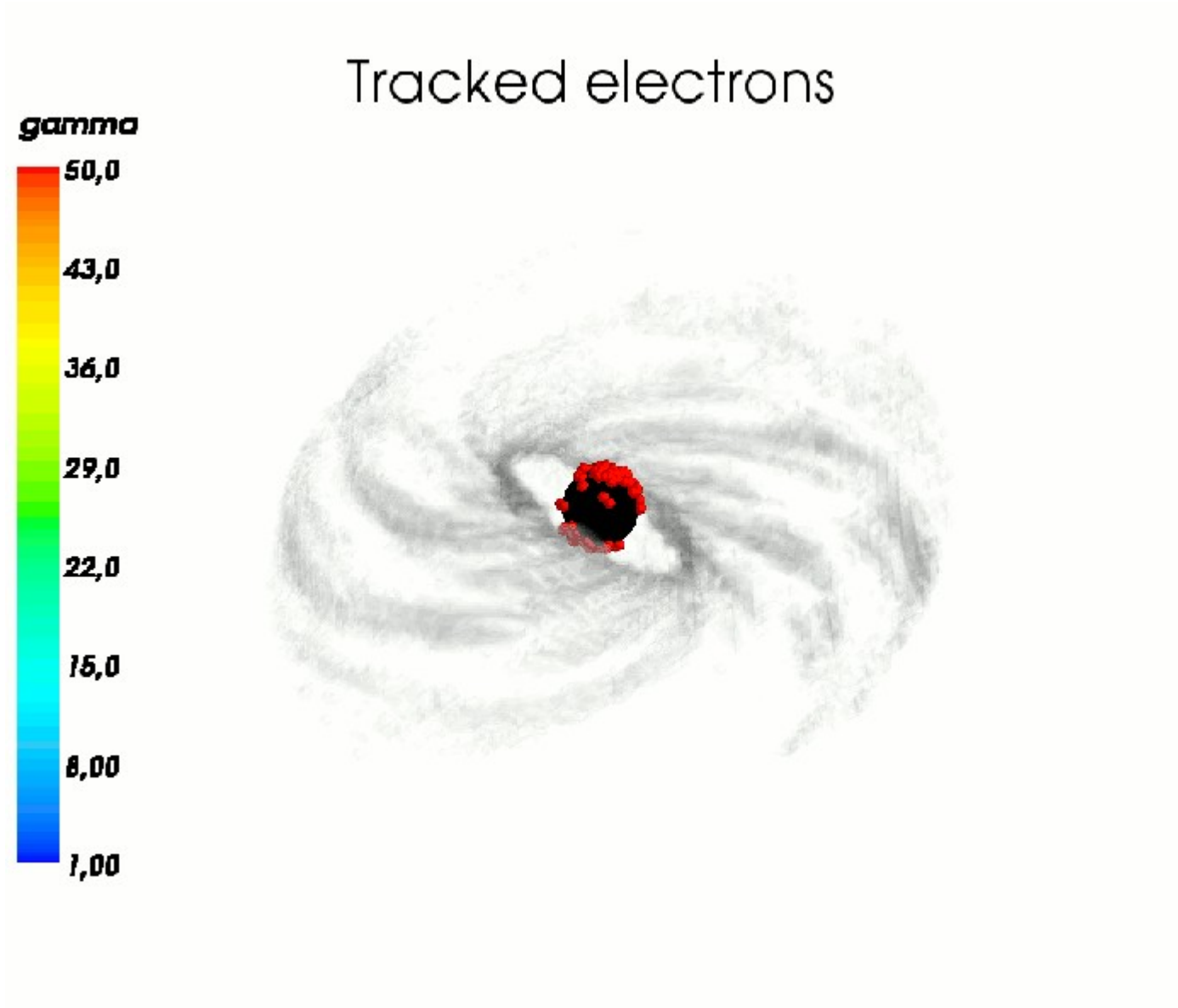


Rotating sprinkler



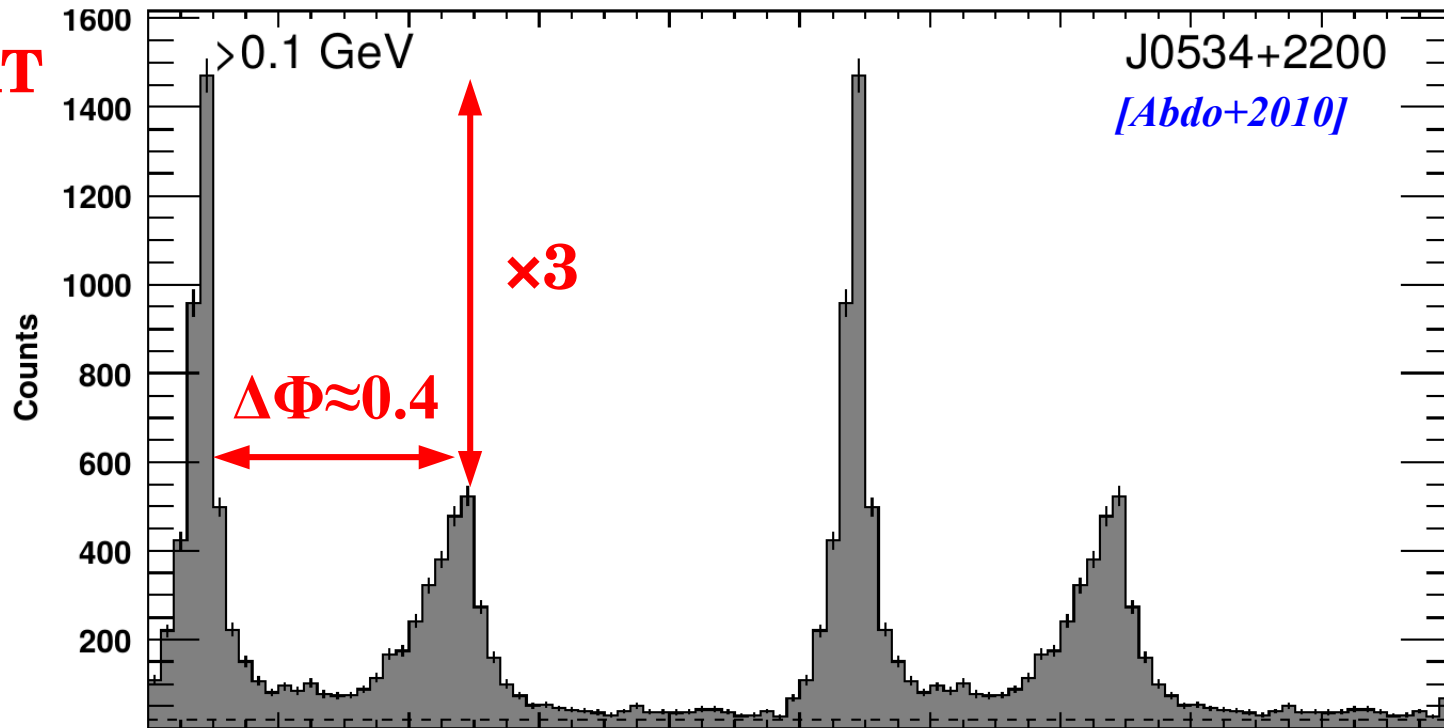
Particle acceleration and origin of the e^+/e^- asymmetry

In the co-rotating frame



Application to the Crab pulsar

Fermi-LAT

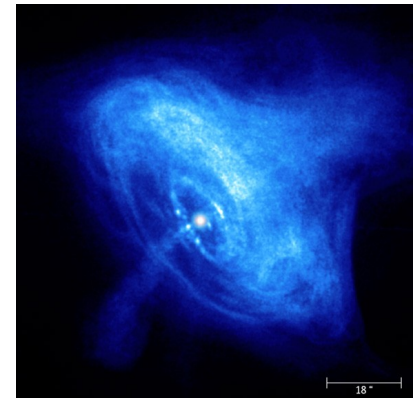
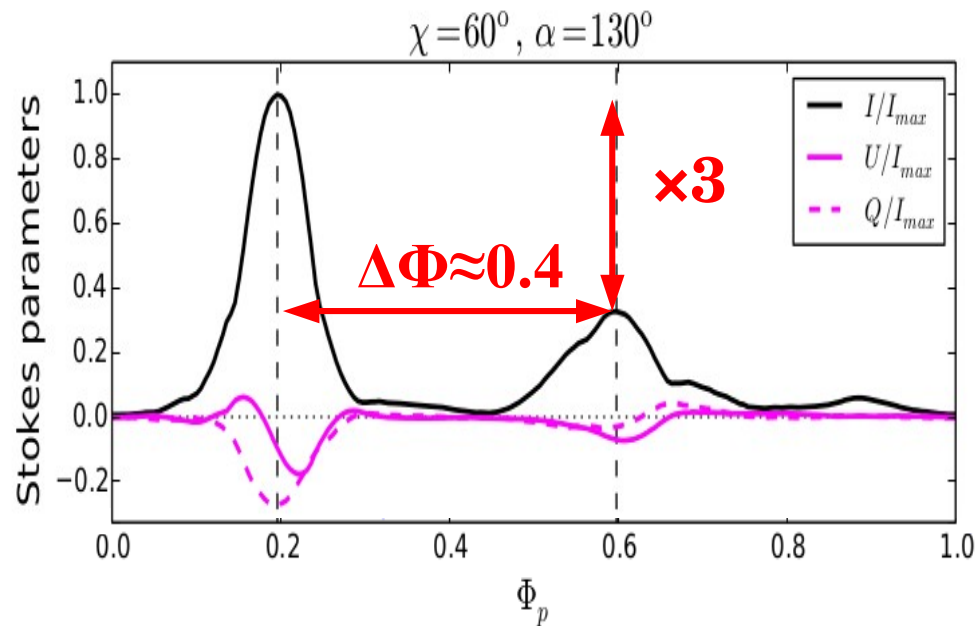


PIC model

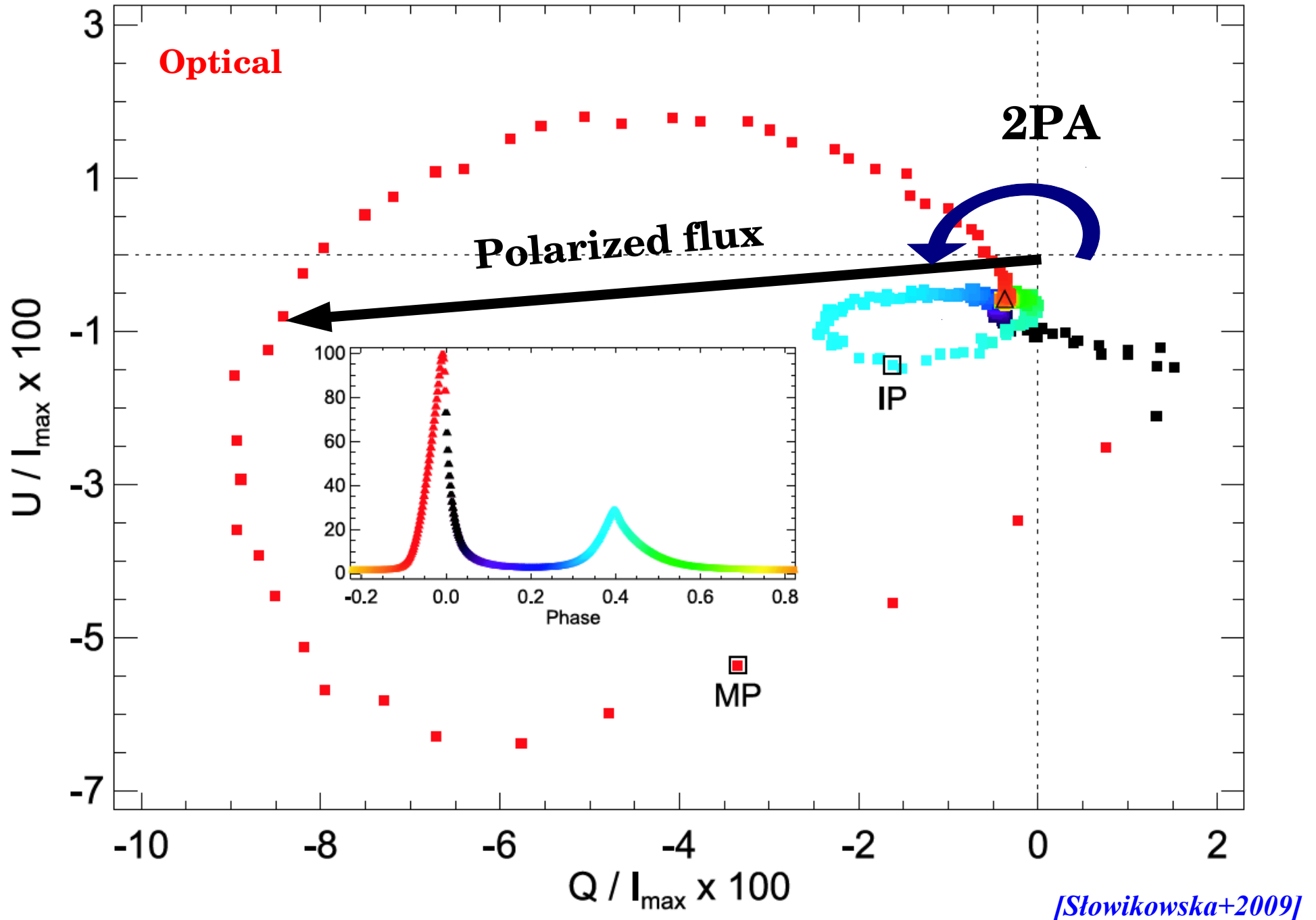
$\chi=60^\circ$, $\alpha=130^\circ$

Consistent with the nebula morphology in **X-rays**

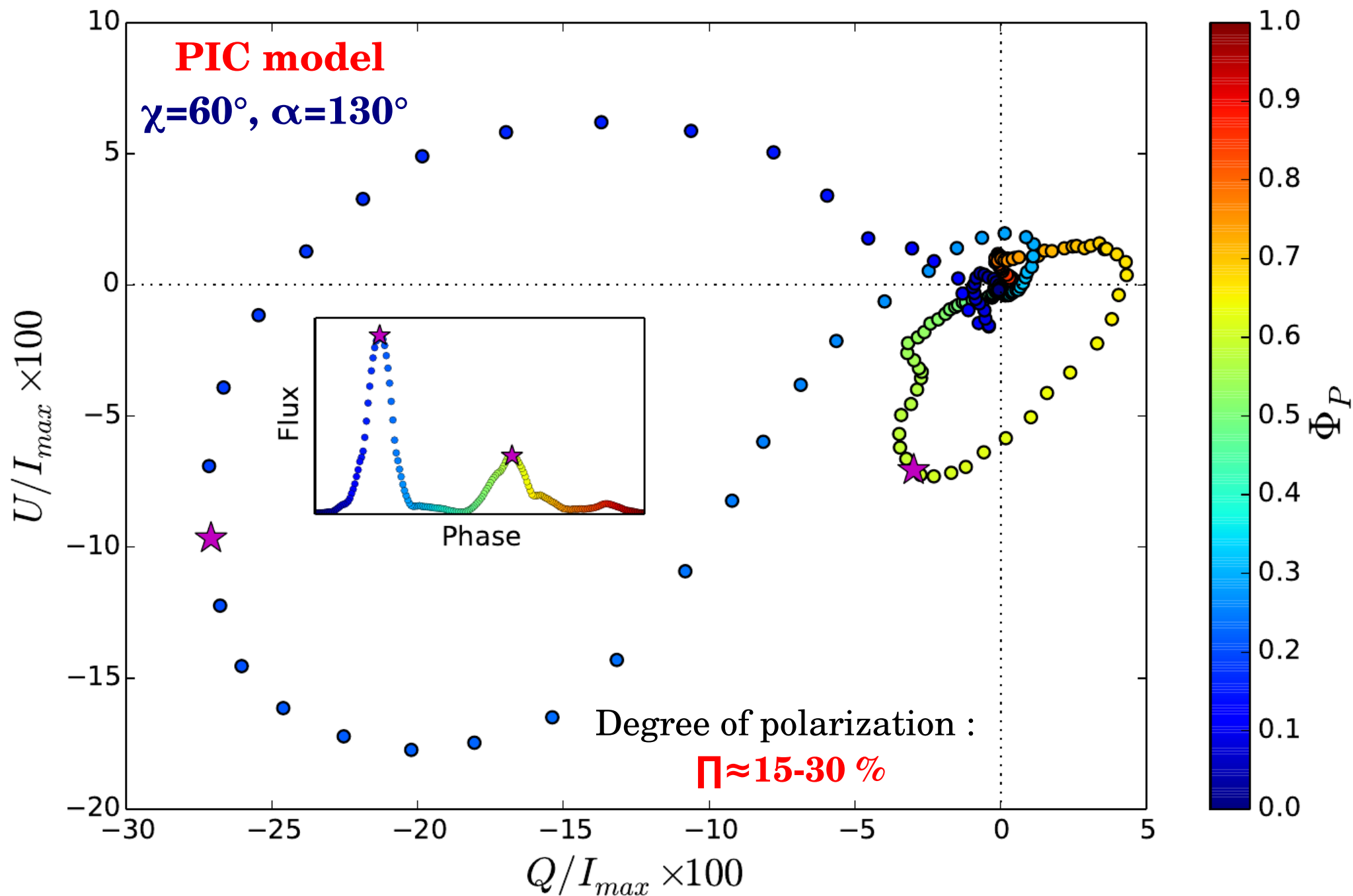
[e.g. Weisskopf+2012]



(Incoherent) Polarization signature : Observations



(Incoherent) Polarization signature : **PIC**

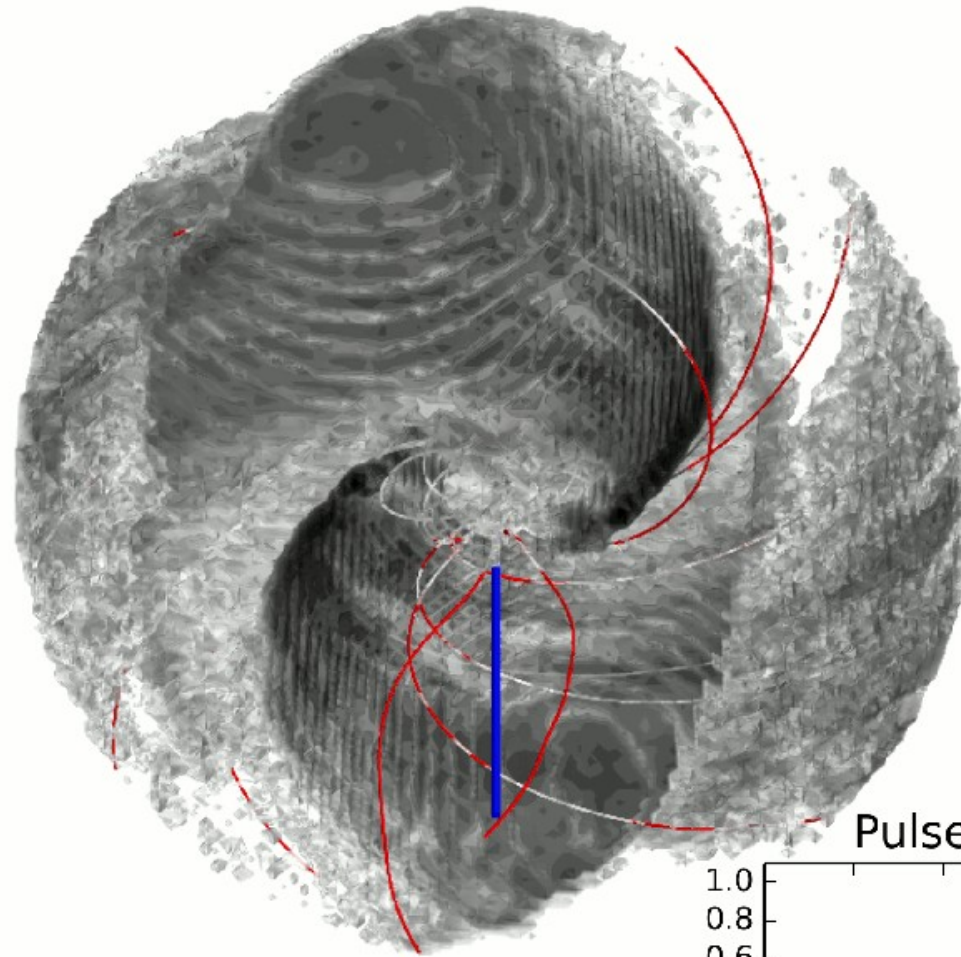


The Crab pulsar as we may see it !

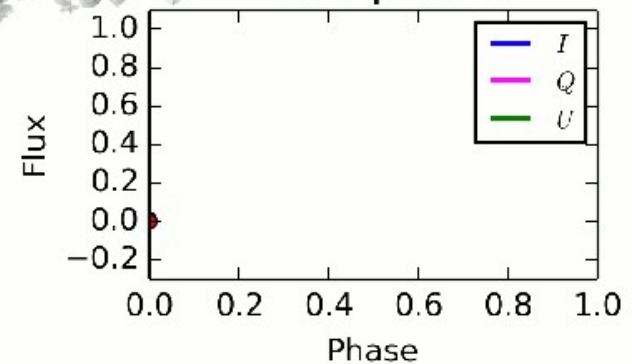
Gray : Total flux (all directions)

Color : Observed flux

$i=60$ - Phase=0.00



Pulse profile



Conclusions

- **Global PIC simulations** is the way to go to solve particle acceleration in **pulsars**, and soon around **black holes**.
- Simulations demonstrate the major role of **relativistic reconnection** in particle acceleration
- High-energy emission could be **synchrotron radiation** from the **current sheet** $> \sim R_{LC}$
- **Pulse profile** and **polarization** provide robust constraints on **Crab pulsar** inclination and viewing angles.
- More work needed to **compare simulations to observations**.
- Origin of the **radio** emission **still unclear**, more physics to capture in the polar-cap discharge ?